

Spectrum of H_2^{18}O in the 2900 to 3400 cm^{-1} Region¹

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Measurements of line center positions of H_2^{18}O in the 2900 to 3400 cm^{-1} region have been made at high resolution. This region contains absorptions of the (020) band and *P*-branch absorptions of the (100) and (001) bands of H_2^{18}O . Values of the energy levels of the (020) state were determined in which ground state energy levels derived by Fraley, Rao, and Jones [*J. Mol. Spectrosc.* 29, 312 (1969)] and Williamson, Rao, and Jones [*J. Mol. Spectrosc.* 40, 372 (1971)] were used in the analysis. A new set of ground state levels was obtained by an iterative procedure.

INTRODUCTION

A knowledge of the positions and strengths of water vapor vibration-rotation lines in the 2900 to 3400 cm^{-1} region is important for the interpretation of atmospheric spectra obtained for the purpose of detecting air pollutants which may be present in the atmosphere and which have strong dipole transition intensities in this spectral interval (for example HCl , NH_3 , NO_2 , C_2H_2 , C_2H_4 , and C_2H_6). High resolution laboratory studies of H_2^{18}O line center measurements in the 3 μm region have been done by Pugh and Rao (1), Camy-Peyret *et al.* (2), and Flaud and Camy-Peyret (3). High resolution measurements of strengths and air-broadened widths of H_2^{16}O lines in the 2950 to 3400 cm^{-1} region have been reported by Toth (4). Comparable measurements of H_2^{18}O in the 2900 to 3400 cm^{-1} region are the subject of this study. The present investigation involves line center measurements and the line strengths will be the subject of a forthcoming publication.

The majority of the H_2^{18}O lines in the 3.3 μm region are of the (020) band with the band center at 3139.054 cm^{-1} . Also in this spectral interval are several *P*-branch lines of the (100) and (001) bands. Previous laboratory investigations of H_2^{18}O line center measurements include an analysis of high resolution spectra of the (100) and (001) bands covering the 3340 to 4030 cm^{-1} region by Fraley *et al.* (5). Williamson *et al.* (6) observed the (010) band in the 1330 to 1967 cm^{-1} region at high resolution. Calculations of positions and rigid-rotor strengths of H_2^{18}O lines in the 2864 to 4435 cm^{-1} region are included in a tabulation of H_2O transitions in the 2.7 μm region reported by Gates *et al.* (7). The calculated line positions of the (020) band (7) are greater than those obtained in this study; the maximum difference is $\sim 1.6 \text{ cm}^{-1}$ for high K_{-1} transitions and the

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minimum difference is on the average 0.04 cm⁻¹ for transitions involving upper and lower state K_{-1} equal to 0 or 1.

EXPERIMENTAL DETAILS

The data were obtained with a 1.8 m Jarrel–Ash grating spectrometer with a 300 lines/mm grating blazed at 5.7 μm in first order. Observations were made in first order for the region 2900 to 3240 cm⁻¹ at a resolution of ~0.07 cm⁻¹, and in second order for the 3240 to 3400 cm⁻¹ region at a resolution of ~0.04 cm⁻¹. The source was a 1000 W quartz-iodine projection lamp and the detector was a PbS element which was cooled to approximately -80°C. A multitraversal cell of 2 m base length was used for all measurements. The foreoptics, source, and detector were housed in a vacuum box which was connected to the vacuum spectrometer and the absorption cell.

The oxygen 18 enriched H₂O sample was obtained from the Bio-Rad Corporation. The stated sample mixture ratio of H₂¹⁸O to H₂¹⁶O was 1-to-1 and the H₂¹⁷O impurity was 0.1% of the sample. Sample pressures were measured with an oil manometer and a capacitance pressure sensor. Sample pressures ranged from 2 to 8 mm Hg and the path lengths ranged from 8 to 40 m with the gas samples at room temperature. The H₂¹⁸O line positions were calibrated from the known H₂¹⁶O absorptions (1, 2, 3).

DATA ANALYSIS

The quantum assignments of the measured H₂¹⁸O lines were determined in the following manner. Approximate locations of several H₂¹⁸O absorptions were determined from the listing of Gates *et al.* (7). By this procedure, the strongest H₂¹⁸O absorptions were easily identified in the spectra. Additional methods were employed to assign weaker transitions. These included: (a) determining approximate locations of H₂¹⁸O lines from a knowledge of the frequency difference between identical transitions of H₂¹⁶O and H₂¹⁸O, (b) comparing the peak absorption of an H₂¹⁸O line to that of the same transition of the H₂¹⁶O molecule, and (c) calculating the line positions of the (100) and (001) bands from the listings given by Fraley *et al.* (5). It was determined that the frequency differences between identical transitions of H₂¹⁶O and H₂¹⁸O ranged between 8 and 20 cm⁻¹ for the (001) and (020) bands and between 2 and 14 cm⁻¹ for the (100) band. It is interesting to note that using a gas sample with 50% H₂¹⁸O and 50% H₂¹⁶O greatly simplified the task of identifying close lying lines since the intensity of a transition for either isotopic specie is comparable except in a very few cases where resonance effects, which alter the normal transition strengths, are different for the two molecules.

RESULTS AND DISCUSSION

Table 1 is a listing of the line numbers, measured line center positions, upper and lower rotational quantum numbers ($JK_{-1}K_1$), ground state energy levels, relative line strengths, and band assignments. The line numbers pertain to the numbering of the absorptions shown in Fig. 1. The relative line strengths S' given in Table 1 were calculated from the expression;

$$S' = g \cdot \nu \cdot \exp(-E''/kT) / (Q \cdot \nu_0), \quad (1)$$

TABLE 1
MEASUREMENTS AND ASSIGNMENTS OF OXYGEN 18 WATER
VAPOR IN THE 2.94 TO 3.45 MICRON SPECTRAL REGION

LINE NUMBER	FREQ -1 CM	ROTATIONAL TRANSITION		FREQ -1 CM	LINE NUMBER	E -1 CM	STRENGTH -1 TEMP-295K	BAND	ROTATIONAL TRANSITION	FREQ -1 CM	LINE NUMBER	ROTATIONAL TRANSITION		E -1 CM	STRENGTH -1 TEMP-295K	BAND
		UPPER STATE	LOWER STATE									UPPER STATE	LOWER STATE			
1	2919.56	7	3	4	8	4	5	020	3	2	1	4	4	482.660	.5226-03	020
2	2921.82	10	1	10	11	0	11	020	5	1	4	6	2	550.447	.1156-02	020
3	2922.92	7	4	3	8	5	4	020	4	3	3	4	4	482.632	.1568-02	020
4	2922.992	6	1	4	7	4	3	020	4	6	0	6	7	583.972	.7199-03	020
5	2922.984	4	1	4	5	2	3	020	46	303.578	6	1	6	583.767	.9582-03	020
6	2924.846	5	2	4	6	3	3	020	47	303.469	9	3	6	583.767	.9582-03	020
7	2924.846	9	0	9	10	1	10	020	48	303.469	4	1	3	583.767	.9582-03	020
8	2924.846	9	1	9	10	1	10	020	49	303.469	4	1	3	583.767	.9582-03	020
9	2924.846	9	1	9	10	1	10	020	50	303.469	4	1	3	583.767	.9582-03	020
10	2924.846	9	1	9	10	1	10	020	51	303.469	4	1	3	583.767	.9582-03	020
11	2924.846	9	1	9	10	1	10	020	52	303.469	4	1	3	583.767	.9582-03	020
12	2924.846	9	1	9	10	1	10	020	53	303.469	4	1	3	583.767	.9582-03	020
13	2924.846	9	1	9	10	1	10	020	54	303.469	4	1	3	583.767	.9582-03	020
14	2924.846	9	1	9	10	1	10	020	55	303.469	4	1	3	583.767	.9582-03	020
15	2924.846	9	1	9	10	1	10	020	56	303.469	4	1	3	583.767	.9582-03	020
16	2924.846	9	1	9	10	1	10	020	57	303.469	4	1	3	583.767	.9582-03	020
17	2924.846	9	1	9	10	1	10	020	58	303.469	4	1	3	583.767	.9582-03	020
18	2924.846	9	1	9	10	1	10	020	59	303.469	4	1	3	583.767	.9582-03	020
19	2924.846	9	1	9	10	1	10	020	60	303.469	4	1	3	583.767	.9582-03	020
20	2924.846	9	1	9	10	1	10	020	61	303.469	4	1	3	583.767	.9582-03	020
21	2924.846	9	1	9	10	1	10	020	62	303.469	4	1	3	583.767	.9582-03	020
22	2924.846	9	1	9	10	1	10	020	63	303.469	4	1	3	583.767	.9582-03	020
23	2924.846	9	1	9	10	1	10	020	64	303.469	4	1	3	583.767	.9582-03	020
24	2924.846	9	1	9	10	1	10	020	65	303.469	4	1	3	583.767	.9582-03	020
25	2924.846	9	1	9	10	1	10	020	66	303.469	4	1	3	583.767	.9582-03	020
26	2924.846	9	1	9	10	1	10	020	67	303.469	4	1	3	583.767	.9582-03	020
27	2924.846	9	1	9	10	1	10	020	68	303.469	4	1	3	583.767	.9582-03	020
28	2924.846	9	1	9	10	1	10	020	69	303.469	4	1	3	583.767	.9582-03	020
29	2924.846	9	1	9	10	1	10	020	70	303.469	4	1	3	583.767	.9582-03	020
30	2924.846	9	1	9	10	1	10	020	71	303.469	4	1	3	583.767	.9582-03	020
31	2924.846	9	1	9	10	1	10	020	72	303.469	4	1	3	583.767	.9582-03	020
32	2924.846	9	1	9	10	1	10	020	73	303.469	4	1	3	583.767	.9582-03	020
33	2924.846	9	1	9	10	1	10	020	74	303.469	4	1	3	583.767	.9582-03	020
34	2924.846	9	1	9	10	1	10	020	75	303.469	4	1	3	583.767	.9582-03	020
35	2924.846	9	1	9	10	1	10	020	76	303.469	4	1	3	583.767	.9582-03	020
36	2924.846	9	1	9	10	1	10	020	77	303.469	4	1	3	583.767	.9582-03	020
37	2924.846	9	1	9	10	1	10	020	78	303.469	4	1	3	583.767	.9582-03	020
38	2924.846	9	1	9	10	1	10	020	79	303.469	4	1	3	583.767	.9582-03	020
39	2924.846	9	1	9	10	1	10	020	80	303.469	4	1	3	583.767	.9582-03	020
40	2924.846	9	1	9	10	1	10	020	81	303.469	4	1	3	583.767	.9582-03	020
41	2924.846	9	1	9	10	1	10	020	82	303.469	4	1	3	583.767	.9582-03	020

TABLE 1 (CONT.)

LINE NUMBER	FREQ CM	FREQ -1	ROTATIONAL TRANSITION		E-1 CM	STRENGTH TEMP-293K	BAND	ROTATIONAL UPPER STATE	ROTATIONAL LOWER STATE	E-1 CM	STRENGTH TEMP-293K	BAND
90	3037.994		5	3	5	4	2	3	3	604.550	-2937-C3	020
91	3038.287		3	2	4	4	1	3	2	782.733	-1407-C2	020
92	3038.632		4	3	4	4	1	3	2	484.632	-1639-C2	020
93	3039.122		4	3	0	882.552	-5837-C3	020	138	3193.807		020
94	3039.790		4	2	4	880.700	-5837-C3	020	139	3198.592		020
95	3110.100		5	3	6	501.216	-3078-C3	020	140	3203.427		020
96	3110.205		0	0	1	36.756	-4756-C2	020	141	3208.262		020
97	3113.192		3	0	7	172.880	-7197-C2	020	142	3213.094		020
98	3113.585		3	0	3	370.620	-5720-C2	020	143	3217.928		020
99	3114.972		6	3	5	752.195	-1942-C3	020	144	3220.552		020
100	3116.566		5	1	4	445.160	-1949-C2	020	145	3223.186		020
101	3116.733		5	2	3	505.727	-1480-C2	020	146	3225.820		020
102	3117.454		2	1	2	733.785	-2953-C2	020	147	3233.943		020
103	3117.629		3	1	3	210.800	-6131-C2	020	148	3233.243		020
104	3110.620		4	1	3	114.460	-1230-C2	020	149	3236.731		020
105	3111.493		6	2	4	553.623	-2237-C3	020	150	3240.902		020
106	3113.078		1	1	2	69.932	-4059-C2	020	151	3244.986		020
107	3113.078		7	2	5	339.561	-2932-C3	020	152	3248.316		020
108	3115.040		8	4	5	1246.366	-3393-C4	020	153	3251.654		020
109	3115.418		5	4	2	1050.990	-3192-C4	020	154	3255.990		020
110	3115.57		5	4	1	733.678	-1595-C3	020	155	3259.326		020
111	3117.251		7	4	3	860.629	-2342-C3	020	156	3263.662		020
112	3120.903		1	0	1	1051.210	-1017-C3	020	157	3267.997		020
113	3121.971		9	3	6	42.024	-1399-01	020	158	3272.333		020
114	3128.792		2	2	1	135.190	-2312-C4	020	159	3276.669		020
115	3135.932		2	2	1	240.900	-1565-C2	020	160	3281.508		020
116	3140.914		6	5	2	485.160	-1967-C2	020	161	3283.700		020
117	3150.452		6	3	1	1033.195	-1119-C3	020	162	3285.167		020
118	3151.486		6	3	7	134.785	-2995-C2	020	163	3285.442		020
119	3154.783		7	3	2	981.900	-2350-C3	020	164	3287.213		020
120	3154.783		3	2	1	232.830	-5825-C2	020	165	3288.400		020
121	3155.503		5	3	2	553.447	-1184-C2	020	166	3292.940		020
122	3156.078		6	3	7	839.561	-2281-C3	020	167	3293.337		020
123	3156.302		4	2	2	325.216	-1185-C2	020	168	3293.337		020
124	3157.243		4	1	3	141.577	-2906-C2	020	169	3293.337		020
125	3161.202		2	0	3	23.756	-1591-01	020	170	3293.337		020
126	3155.098		1	1	0	1001.709	-1316-C3	020	171	3293.337		020
127	3166.733		7	3	6	445.355	-1985-C2	020	172	3293.337		020
128	3167.120		5	2	3	61.470	-7770-C3	020	173	3293.337		020
129	3167.900		4	3	1	814.177	-1254-C2	020	174	3293.337		020
130	3169.39		3	1	4	134.460	-3544-C4	100	175	3293.337		020
131	3170.44		7	2	5	1246.366	-2809-C5	100	176	3293.337		020
132	3170.89		9	2	8	153.358	-4136-C2	020	177	3293.337		020
133	3172.311		2	1	2	69.930	-4136-C2	020	178	3293.337		020
134	3172.474		2	0	2	36.750	-4863-C2	020	179	3293.337		020

TABLE 1 (CONT.)

LINE NUMBER	FREQ CH	ROTATIONAL UPPER STATE	ROTATIONAL LOWER STATE	E -1 CH	STRENGTH TEMP=295K	BAND	LINE NUMBER	FREQ CH	ROTATIONAL UPPER STATE	ROTATIONAL LOWER STATE	E -1 CH	STRENGTH TEMP=295K	BAND
182	3273-180	3 3 0	3 2 1	210-800	6440-02	020	224	3328-563	9 3 6	10 4 7	1574-835	7277-05	100
183	3274-083	8 4 5	9 5 4	1468-567	1200-04	100	225	3328-902	7 4 3	7 3 4	839-561	3050-03	020
184	3275-359	6 2 5	6 1 6	445-355	2053-02	020	226	3330-004	9 1 8	9 0 9	916-250	2093-03	020
185	3277-093	8 3 6	9 4 5	1355-190	2087-04	100	227	3332-595	5 5 1	6 6 0	1033-195	3404-04	100
186	3278-295	7 0 7	6 1 6	445-355	2054-02	020	228	3332-695	5 5 0	6 6 1	1033-195	3404-04	100
187	3278-295	3 2 2	2 1 1	184-790	3786-02	020	229	3335-535	7 0 7	8 2 6	980-230	4303-04	001
188	3279-361	6 6 1	7 7 0	974-980	1860-04	100	230	3337-005	7 0 7	6 6 1	591-483	4366-03	020
189	3279-620	7 5 2	8 6 3	1378-980	6200-05	100	231	3337-533	6 4 2	6 3 3	656-623	2464-03	020
190	3280-550	7 1 6	7 0 6	444-860	1681-04	100	232	3339-526	6 3 3	7 5 2	181-577	3070-02	020
191	3282-953	4 3 2	4 2 3	503-767	1047-02	020	233	3341-597	11 0 11	10 10	1051-210	8143-04	001
192	3284-047	6 1 5	5 2 4	444-177	4208-02	020	234	3341-947	11 1 11	10 10	1109-770	8143-04	020
193	3285-166	7 3 4	6 5 3	751-040	4638-03	020	235	3343-501	5 4 1	5 3 2	505-727	2731-04	020
194	3288-370	5 3 3	5 2 4	880-079	4472-03	020	236	3346-508	8 3 5	9 4 6	1336-680	7649-05	100
195	3289-048	7 3 5	8 5 4	414-177	7597-03	020	237	3347-846	3 3 0	3 0 3	135-344	9471-02	020
196	3290-075	5 1 4	6 4 3	1246-359	3476-04	001	238	3347-767	5 3 3	6 5 2	880-079	2112-03	001
197	3292-77	5 4 2	6 6 1	1033-195	3932-03	100	239	3347-810	4 4 1	4 3 2	379-493	2896-02	020
198	3295-180	4 2 3	3 1 2	172-888	7759-02	020	240	3348-563	5 4 2	5 3 3	500-595	5343-03	020
199	3295-559	7 2 6	8 5 3	1047-517	3142-04	100	241	3350-066	3 3 1	2 2 0	134-785	3183-02	020
200	3297-331	6 3 4	6 2 5	583-767	1051-02	020	242	3350-047	6 2 5	7 3 4	839-561	2640-03	100
201	3297-331	6 3 4	6 2 5	583-767	1051-02	020	243	3350-246	6 4 3	6 3 4	645-387	7913-03	020
202	3299-310	7 2 1	2 1 2	78-935	1238-02	020	244	3350-507	3 3 0	2 2 1	133-480	9613-02	020
203	3302-360	7 4 4	8 5 3	1247-200	1188-04	100	245	3352-597	8 2 6	9 4 5	1355-190	2083-04	001
204	3306-01	8 1 6	8 0 8	740-530	1633-03	020	246	3352-697	5 3 2	6 5 1	840-121	7047-04	001
205	3306-380	6 1 6	7 2 5	780-440	3476-03	100	247	3353-440	8 2 7	7 1 6	701-697	6018-03	020
206	3306-277	6 5 2	7 6 2	1284-186	4399-04	100	248	3353-718	7 4 4	7 3 5	812-753	1167-03	020
207	3307-249	7 2 5	6 3 4	645-387	7612-03	020	249	3354-668	4 0 4	5 4 3	604-756	8103-03	001
208	3308-65	9 2 7	9 1 8	174-779	9622-04	020	250	3356-286	6 3 4	7 4 3	523-698	1737-03	100
209	3308-65	7 3 5	7 2 6	706-608	1333-03	020	251	3358-084	6 2 5	7 4 4	1116-620	6640-04	100
210	3311-322	9 0 9	8 1 6	741-000	4908-03	020	252	3358-945	6 2 5	7 4 4	921-910	5758-04	001
211	3311-614	9 1 9	8 0 8	740-530	1636-03	020	253	3359-597	8 4 5	8 3 6	1001-709	1359-03	020
212	3312-496	7 4 3	8 5 3	1246-369	3508-04	100	254	3362-211	5 4 1	6 5 2	840-079	2174-03	100
213	3313-878	7 1 6	6 2 5	550-447	1244-02	020	255	3362-873	4 0 4	5 3 3	900-595	7247-04	100
214	3314-141	8 2 7	8 1 8	741-000	4910-03	020	256	3366-236	4 0 4	5 3 3	500-595	4619-03	100
215	3314-462	7 1 6	8 3 6	1001-709	1253-03	001	257	3366-889	6 1 5	7 2 4	812-753	9831-04	001
216	3316-593	7 2 6	8 4 5	1116-620	6602-04	001	258	3367-454	5 1 5	6 2 4	601-246	2828-03	100
217	3319-694	6 3 4	7 5 3	1050-990	3032-04	001	259	3370-604	12 1 12	13 0 13	1800-800	2452-05	100
218	3320-141	7 3 5	8 4 4	1126-980	2151-04	100	260	3371-800	9 2 8	8 1 7	879-481	2842-05	100
219	3322-262	5 0 5	6 3 4	645-387	6749-03	100	261	3372-211	11 1 10	12 2 11	1767-000	2082-05	020
220	3322-348	6 2 5	5 1 4	398-372	2618-02	020	262	3374-744	4 3 2	5 4 1	733-573	1648-03	001
221	3324-759	10 0 10	9 1 9	946-300	4947-03	020	263	3375-112	6 3 3	7 4 4	921-910	5932-04	100
222	3324-871	10 1 10	9 0 9	916-250	2097-03	020	264	3376-289	4 3 1	5 4 0	733-578	4349-03	001
223	3324-911	6 5 1	7 5 2	1051-210	1086-03	020	265	3377-229	4 3 1	3 2 2	204-763	2281-02	020
224	3328-663	6 5 1	7 5 2	1051-210	1086-03	020	266	3381-668	9 2 8	8 3 6	1001-709	1408-03	020
							267	3381-900	5 3 2	5 0 5	324-044	3030-02	020
							268	3384-771	7 1 6	6 3 4	1047-317	3147-04	001
							269	3385-131	7 1 6	6 3 4	1126-980	2139-04	001

TABLE 1 (CONT.)

LINE NUMBER	FREQ -1 CM	ROTATIONAL TRANSITION		E -1 CM	STRENGTH TEMP=295K	BAND
		UPPER STATE	LOWER STATE			
271	3386.348	9 2 7	10 3 6	1440.295	.1424-C4	100
272	3387.374	5 3 3	6 4 2	752.195	.1362-03	100
273	3387.638	4 4 0	5 5 1	733.673	.1451-C3	100
274	3387.711	4 4 1	5 5 0	733.679	.4474-C3	100
275	3388.081	5 3 3	4 2 2	314.460	.1340-C2	020
276	3388.538	5 2 3	4 1 4	223.930	.6257-C2	020
277	3390.264	10 2 9	9 1 8	1074.779	.9860-C4	020
278	3391.439	5 3 2	6 4 3	751.040	.4115-C3	100
279	3394.374	10 1 9	11 2 10	1518.750	.3245-05	100
280	3394.595	11 0 11	12 1 12	1551.190	.8312-05	100
280	3394.695	11 1 11	12 0 12	1551.190	.2771-05	100
281	3395.105	10 2 9	11 1 10	1518.550	.9749-C5	100
282	3397.141	5 2 4	6 3 3	658.623	.2157-C3	100
283	3398.975	6 0 6	7 2 5	780.440	.3495-C3	001
284	3399.219	5 2 4	6 4 3	751.040	.4023-C3	001
285	3401.705	8 2 6	9 3 7	1211.100	.1458-C4	100
286	3402.626	6 3 4	5 2 3	445.160	.2134-C2	020
287	3404.294	3 0 3	4 3 2	379.203	.2533-C2	100
288	3407.329	5 3 2	4 2 3	298.629	.4368-C2	020

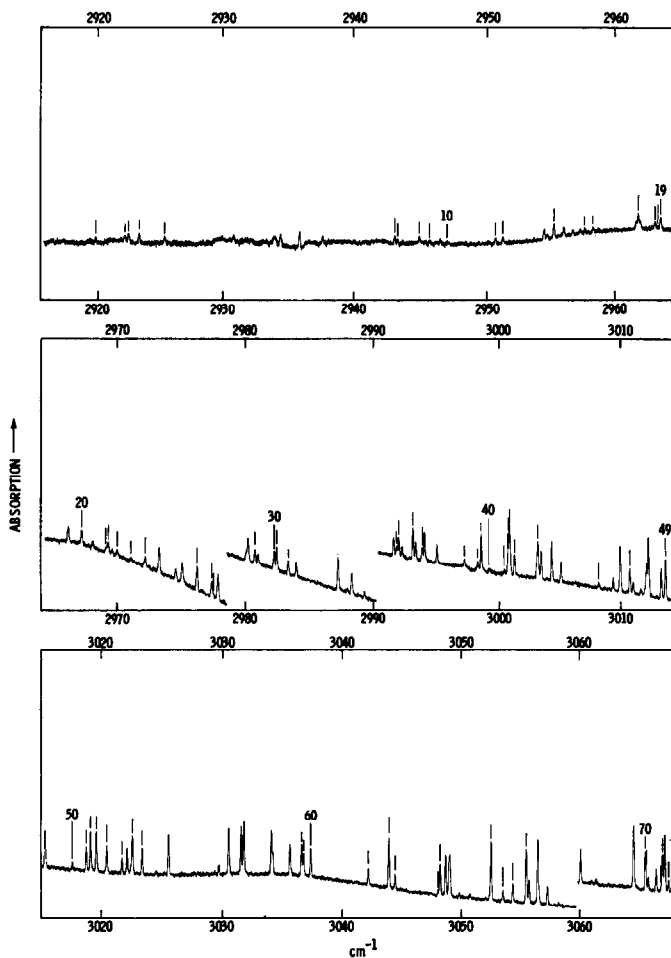


FIG. 1. Scan of the 2920 to 3407 cm⁻¹ region of H₂¹⁸O and H₂¹⁶O. The sample pressure was 4.7 mm Hg and the path was 40 m. The isotopic ratio of the water vapor sample was 1-to-1 for H₂¹⁸O to H₂¹⁶O. The stroke marks denote the H₂¹⁸O lines and only these are numbered.

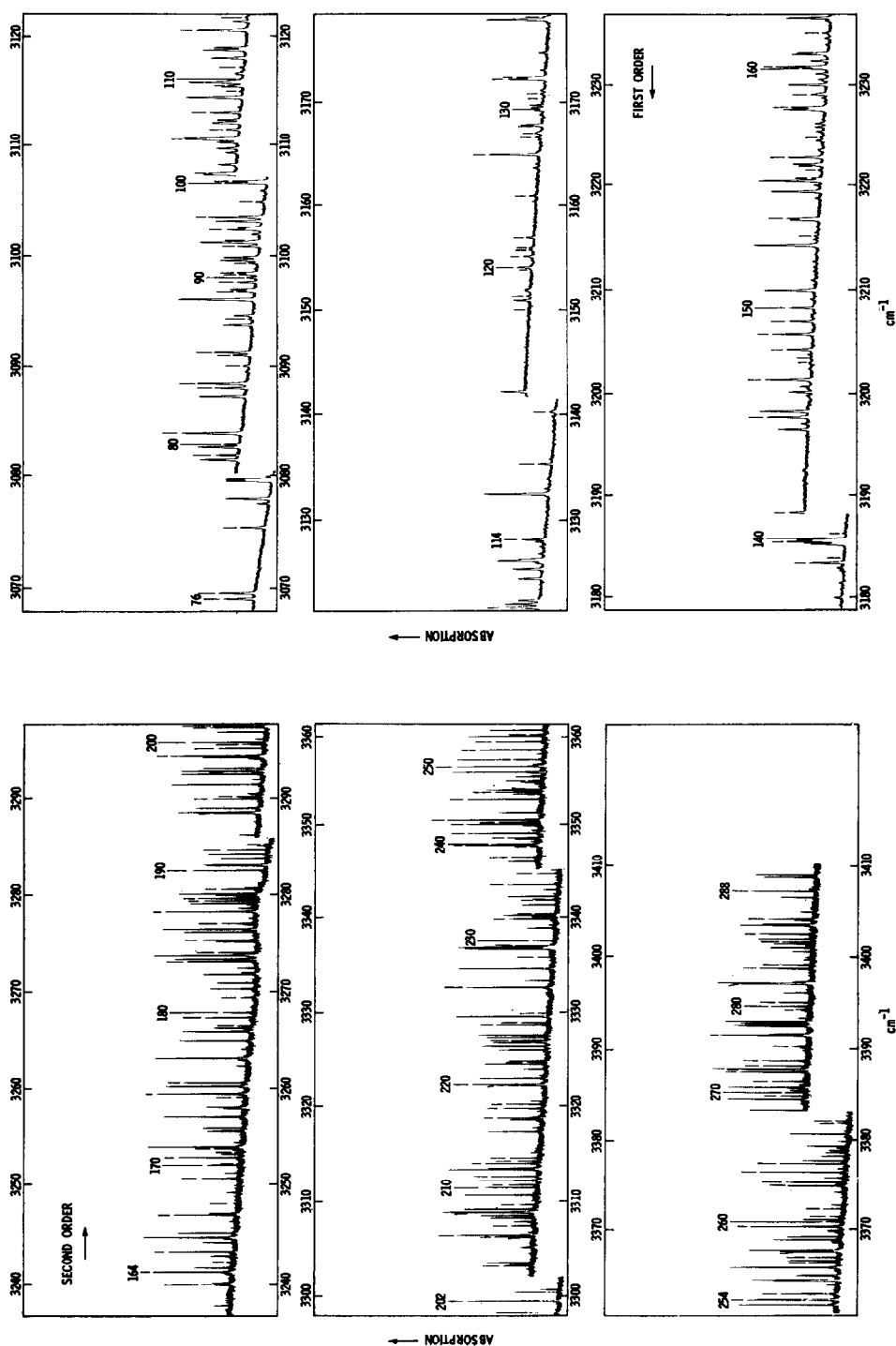


FIG. 1. (Continued)

TABLE 2
Energy Levels (cm⁻¹) of the Ground State (000) and the (020) State of H₂¹⁸O

J K _a K _c	000			020	J K _a K _c	000			020
	This Work	Fraley et al. ^a	Williamson et al. ^b			This Work	Fraley et al. ^a	Williamson et al. ^b	
0 0 0	0	0	0	3139.054	8 0 8	740.930	740.940	740.947	3879.159
1 0 1	23.756	23.756	23.759	3162.823	8 1 8	741.000	741.013	741.009	3879.557
1 1 1	36.750	36.751	36.747	3183.004	8 1 7	879.481	879.481	879.482	4046.945
1 1 0	42.024	42.024	42.023	3188.860	8 2 7	881.900	881.902	881.895	4055.141
2 0 2	69.930	69.932	69.944	3209.228	8 2 6	980.230	980.230	980.227	4206.661
2 1 2	78.995	78.995	78.988	3224.719	8 3 6	1001.709	1001.718	1001.709	4261.408
2 1 1	94.790	94.790	94.790	3242.240	8 3 5	1047.317	1047.317	1047.314	
2 2 1	133.480	133.479	133.482	3301.676	8 4 5	1116.620	1116.635	1116.620	
2 2 0	134.785	134.785	134.784	3302.716	8 4 4	1126.480	1126.433	1126.437	
3 0 3	136.344	136.344	136.344	3276.274	8 5 4	1246.369	1246.319		
3 1 3	141.577	141.576	141.581	3266.604	8 5 3	1247.20	1247.234		
3 1 2	172.888	172.887	172.891	3321.429	9 0 9	916.250		916.261	4052.315
3 2 2	204.763	204.762	204.764	3373.081	9 1 9	916.300		916.341	4052.55
3 2 1	210.800	210.800	210.799	3378.303	9 1 8	1074.779	1074.779	1074.777	4246.259
3 3 1	282.093	282.093	282.093	3483.850	9 2 8	1075.920	1075.932	1075.922	4250.89
3 3 0	282.304	282.304	282.305	3483.985	9 2 7	1198.190	1198.194	1198.187	4383.38
4 0 4	221.237	221.237	221.234	3361.95	9 3 7		1211.190	1211.190	
4 1 4	223.830	223.830	223.833	3368.041	9 3 6	1279.800	1279.822	1279.830	4477.16
4 1 3	274.793	274.811	274.793	3425.183	9 4 6	1334.68			
4 2 3	298.629	298.629	298.622	3467.278	9 4 5	1355.19			
4 2 2	314.460	314.460	314.461	3481.497	10 0 10	1109.808			4243.17
4 3 2	379.293	379.293	379.293	3581.077	10 1 10	1109.770			4243.270
4 3 1	380.700	380.700	380.702	3581.986	10 1 9	1287.727			
4 4 1	482.632	482.632	482.638	3727.199	10 2 9	1288.264			4465.043
4 4 0	482.660	482.660	482.672	3727.208	10 2 8	1433.061			
5 0 5	324.044	324.026	324.034	3465.180	10 3 8	1440.295			
5 1 5	325.216	325.194	325.216	3468.454	10 3 7	1534.368			
5 1 4	398.372	398.371	398.384	3551.730	11 0 11	1321.44			4451.65
5 2 4	414.177	414.177	414.176	3583.445	11 1 11				4451.76
5 2 3	445.160	445.160	445.155	3612.465	11 1 10	1518.55			
5 3 3	500.595	500.604	500.594	3702.541	12 1 12	1551.19			4677.85
5 3 2	505.727	505.726	505.745	3705.950					
5 4 2	604.550	604.549	604.564	3849.157					
5 4 1	604.796	604.796	604.797	3849.277					
5 5 1	733.673	733.708		4027.45					
5 5 0	733.678	733.712		4027.45					
6 0 6	444.860	444.848	444.861	3585.675	a. See Ref (5)				
6 1 6	445.355	445.354	445.364	3587.347	b. See Ref (6)				
6 1 5	541.183	541.183	541.169	3698.827					
6 2 5	550.447	550.447	550.456	3720.710					
6 2 4	601.246	601.246	601.252	3770.096					
6 3 4	645.387	645.377	645.377	3847.785					
6 3 3	658.623	658.601	658.623	3857.064					
6 4 3	751.040	751.031	751.046	3995.637					
6 4 2	752.195	752.195	752.214	3996.206					
6 5 2	880.079	880.100	880.079	4174.10					
6 5 1	880.121	880.146	880.121	4174.11					
6 6 1	1033.195	1033.548	1033.495	4379.87					
6 6 0	1033.195	1033.548	1033.495						
7 0 7	583.767	583.767	583.757	3723.643					
7 1 7	583.972	583.972	583.972	3724.485					
7 1 6	701.697	701.697	701.692	3864.321					
7 2 6	706.608	706.608	706.608	3878.187					
7 2 5	780.440	780.428	780.441	3952.637					
7 3 5	812.753	812.753	812.746	4016.130					
7 3 4	839.561	839.561	839.564	4036.200					
7 4 4	921.910	921.908	921.927	4166.471					
7 4 3	925.698	925.698	925.688	4168.458					
7 5 3	1050.990	1051.036	1051.010						
7 5 2	1051.210	1051.334	1051.308						
7 6 2	1204.172								
7 6 1	1204.186								
7 7 1	1378.98								
7 7 0	1378.98								

where g is the statistical weighting factor for the ground state level (same as H₂¹⁶O), ν is the line center frequency, E'' is the ground state energy level, k is Boltzmann's constant, Q is the rotational partition function and ν_0 is the band center frequency. Values of S' are of little value for the purpose of analyzing atmospheric spectra but they were included in Table 1 because they are required in determining the vibrational band

TABLE 3

Positions (cm^{-1}) of H_2^{18}O and H_2^{16}O Lines which were Blended in the Spectral Data

H_2^{16}O				H_2^{18}O			
Position ^a	Upper J K ₋₁ K ₁	Lower J K ₋₁ K ₁	Band	Position ^b	Upper J K ₋₁ K ₁	Lower J K ₋₁ K ₁	Band
2935.193	4 1 4	5 2 3	020	2935.154	6 3 3	7 4 4	020
2980.387	5 4 1	6 5 2	020	2980.362	8 2 7	9 1 8	020
3087.192	6 2 5	6 3 4	020	3087.16	4 0 4	4 1 3	020
3095.945	1 0 1	2 1 2	020	3095.999	3 2 1	3 3 0	020
3101.156	2 1 2	3 0 3	020	3101.154	5 3 2	5 4 1	020
3110.594	4 3 1	4 4 0	020	3110.502	7 3 4	7 4 3	020
3114.493	0 0 0	1 1 1	020	3114.438	2 0 2	2 1 1	020
3199.359	6 4 2	7 3 5	020	3199.404	4 2 2	3 3 1	020
3214.123	2 1 2	1 0 1	020	3214.093	5 2 3	5 1 4	020
3220.442	4 2 2	4 1 3	020	{ 3220.37	4 0 4	3 1 3	020
3223.326	7 2 5	8 1 8	020	{ 3220.420	4 1 3	3 2 2	020
3260.427	5 1 5	4 0 4	020	3223.318	5 3 2	4 4 1	020
3262.517	6 1 5	7 4 4	100	3260.459	6 0 6	5 1 5	020
3263.275	7 2 5	7 1 6	020	3262.533	6 4 2	5 5 1	020
3266.101	6 5 2	7 4 3	020	3263.303	6 1 6	5 0 5	020
3266.086	8 3 6	9 5 5	001	3266.026	2 2 0	1 1 1	020
3272.518	4 3 2	5 0 5	020	3272.518	8 0 8	9 2 7	001
3278.841	9 1 8	10 3 7	001	3278.81	6 6 1	7 7 0	100
3293.093	7 1 6	7 0 7	020	3293.089	5 4 1	6 6 0	001
3294.210	3 3 1	3 2 2	020	3294.215	7 2 6	7 1 7	020
3326.797	7 1 7	8 3 6	001	3326.827	8 1 7	9 3 6	001
3329.644	7 2 6	8 4 5	001	3329.680	6 4 3	7 5 2	100
3336.897	9 3 6	10 4 7	100	3336.926	6 4 2	7 5 3	100
3340.298	10 1 10	9 0 9	020	3340.337	8 1 7	7 2 6	020
3364.347	3 3 1	2 2 0	020	3364.359	9 1 8	8 2 7	020

a. See Ref. (3)

b. Calculated from energy levels given in this work and in Ref (5)

strength S_v , and F , a factor which accounts for the vibration-rotation effects, from laboratory spectra used to determine values of the absolute line strength S . S is expressed as

$$S = S_v \cdot S' \cdot F \cdot L, \quad (2)$$

where L is the rigid-rotor transition intensity. Values of E'' given in Table 1 were determined from the analysis of the present data which is the subject of the following discussion.

Values of the energy levels of the ground state and the (020) state are presented in Table 2. Also included in Table 2 are values of E'' reported in the work of Fraley *et al.* (5) and Williamson *et al.* (6). Values given in the first and last columns of Table 2 were determined by the method of combination differences using ground state levels given

in Refs. (5) and (6) as an initial set of E'' and therefore deriving an initial set of energy levels for the (020) state from the measured line positions. The initial set of upper state levels were then used to determine new values for the ground state levels. This process was repeated several times. This technique was used for the (020) band having 2 or more observed lines with identical upper state quantum numbers. For levels of the (020) state which are involved in only one observed transition, such as the 000 ← 111 transition, the upper level was calculated from the measured line frequency and the ground state level, obtained by the method given above. The same procedure was used to determine ground state levels which were involved in only one observed transition. For a few observed lines, it was not possible to determine values of either the upper state or lower state levels such as those listed as line numbers 141, 260, and 262 in Table 1. For these lines an approximate value of E'' was entered in Table 1. The ground state levels obtained in this work are, on the average, in good agreement with those given in Refs. (5) and (6) with the exceptions being the levels 660, 661, and 752.

Several H₂¹⁸O lines were blended with H₂¹⁶O lines in the spectra to an extent that these line positions could not be measured with very much accuracy. Table 3 is a listing of these lines for both isotopic species along with their quantum and band assignments. The H₂¹⁶O frequencies are those given by Flaud and Camy-Peyret (3) and the H₂¹⁸O values were calculated from the levels of the ground and (020) states derived in this work (given in Table 2), and also from the (001) and (100) levels given by Fraley *et al.* (5).

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REFERENCES

1. L. A. PUGH AND K. NARAHARI RAO, *J. Mol. Spectrosc.* **47**, 403 (1973).
2. C. CAMY-PEYRET, J. M. FLAUD, G. GUELACHVILI, AND C. AMIOT, *Mol. Physics* **26**, 825 (1973).
3. J. M. FLAUD AND C. CAMY-PEYRET, *Mol. Physics* **26**, 811 (1973).
4. R. A. TOTH, *J. Quant. Spectrosc. Radiat. Transfer* **13**, 1127 (1973).
5. P. E. FRALEY, K. NARAHARI RAO, AND L. H. JONES, *J. Mol. Spectrosc.* **29**, 312 (1969).
6. J. G. WILLIAMSON, K. NARAHARI RAO, AND L. H. JONES, *J. Mol. Spectrosc.* **40**, 372 (1971).
7. D. M. GATES, R. F. CALFEE, D. W. HANSEN, AND W. S. BENEDICT, *Natl. Bur. Stand. Monograph* **71** (1964).