



Contents lists available at ScienceDirect

Journal of Quantitative Spectroscopy and Radiative Transfer

journal homepage: www.elsevier.com/locate/jqsrt

Empirical rovibrational energy levels for nitrous oxide

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ARTICLE INFO

Keywords:

Rovibrational energy levels

N₂O

MARVEL

ABSTRACT

A survey of the huge number of measured rovibrational transitions of the ¹⁴N₂¹⁶O isotopologue of nitrous oxide is performed which either confirms the positions, the assignments, and the uncertainties of the measurements or refutes at least one of them. Data from 95 literature sources are analyzed and their assignments adjusted to a uniform set of polyads and associated counting numbers. This is an important result of the present study and this canonical set of vibrational state assignments is recommended for future studies. The adjusted list of 67 930 transitions (43 246 unique ones) then underwent a thorough MARVEL (Measured Active Rotational–Vibrational Energy Levels) analysis, yielding 17 561 empirical rovibrational energy levels. Uncertainties for these levels are determined using a newly implemented bootstrap approach. The bootstrap uncertainties indicate that the uncertainties for about 1.5% of the energy levels had to be increased significantly, often by more than 10 times compared to previous level uncertainty estimates. This study yields empirical values for 78 band origins of ¹⁴N₂¹⁶O for states with $\ell = 0$, where ℓ is the vibrational angular momentum quantum number. The measured transitions and the empirical energy levels are compared to the SISAM and the recent NOSL-296 line lists with the result that while the overall agreement is good, there are still a number of issues requiring further careful experimental and modeling studies.

1. Introduction

Nitrous oxide, commonly known as laughing gas due to its medical applications in surgery and dentistry, is a linear asymmetric triatomic molecule with the formula N₂O. N₂O is a trace atmospheric species on Earth, whose atmospheric concentration has been slowly growing in recent decades and it is thought to be a current major remaining destroyer of stratospheric ozone [1]. N₂O has been proposed as an observable species in Earth-like exoplanets [2] and its spectrum has been considered as a possible bio-signature [3]. Therefore, N₂O is included in the list of target species in exoplanet characterization missions [4,5].

The rotation–vibration spectrum of the linear N₂O molecule has been thoroughly investigated [6–180]. These studies often addressed issues related to the atmospheric presence of N₂O and also involved fundamental questions related to the dynamics and spectroscopy of the molecule itself. High-accuracy studies of the spectra of N₂O have also played an important role in providing infrared frequency calibration standards [20,62,66,68–70,84,108].

This work concentrates on the main isotopologue of nitrous oxide, ¹⁴N₂¹⁶O. There have been many experimental studies of the spectrum of ¹⁴N₂¹⁶O yielding high-resolution (rotationally-resolved) data that

could be used during the present study. There are a similarly large number of papers [8,11,13–16,19,21,25,26,29,34–37,39–42,45,47,48,50,52,53,61,62,65,75,76,78,79,83,84,86–92,94–96,98,103,104,106,109,112,115,117,121–123,126,130,131,135,138,139,143,144,147,149,151,152,154,160–163,165–167,171,172,177] which do not provide transition data on N₂O of direct use for the present study. Importantly, some of these papers provide line list compilations, both (semi-)empirical ones [125,151,179,181,182] and those based on the use of variational nuclear-motion calculations [177]. The most recent line list relevant for the present study is NOSL-296 [179], which was published while this work was nearing completion.

There are a number of theoretical studies, performed at various levels of sophistication, related to the representation of the potential energy surface [183–189] and the (ro)vibrational spectra [177,188,190–192] of nitrous oxide. These studies, the best of which yield a very large set of rovibrational energies, though with relatively large discrepancies with respect to the experimental information, and enormous line lists, are important to understand the rotational–vibrational spectroscopy of N₂O and, in particular, the ordering of its vibrational states.

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<https://doi.org/10.1016/j.jqsrt.2024.108902>

Received 1 August 2023; Received in revised form 8 January 2024; Accepted 8 January 2024

Available online 19 January 2024

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At the beginning of the project described here, we collected all the experimental rovibrational transitions data available for $^{14}\text{N}_2^{16}\text{O}$, with the available assignments and uncertainties, and placed them into a database. This initial phase identified issues with bands given different vibrational assignments in different papers. It was therefore necessary to develop a unique set of vibrational labels to allow the data to be processed. Following this relabeling, a spectroscopic network [193–195] was formed from the lines observed. This allowed the validation of the vast majority of the measured transitions. Occasionally, the same procedure allowed the identification of conflicting or incorrect measurements. After the survey of the measured transitions and the cleansing of the database, we calculated empirical rovibrational energies for the states involved in the measured transitions with the help of the latest version of the Measured Active Rotational–Vibrational Energy Levels (MARVEL) algorithm and code [193,195–197]. The set of measured transitions and the empirical rovibrational energy levels obtained are made available in the Supplementary Information accompanying this paper. The empirical rovibrational energy levels deduced at the end of this study are compared to previous literature results [125,179], revealing several issues.

2. Theoretical details

2.1. MARVEL

The MARVEL algorithm, used extensively during this study, is based on the theory of spectroscopic networks (SN) [193–195]. The SN of a molecule is a graph $G(V, E)$, in which the vertex set V represents the discrete quantum states of the molecule, and the edge set E corresponds to (allowed) transitions between the quantum states. When a large number of accurately measured and assigned, interconnected transitions are available for a given isotopologue of a molecule, MARVEL yields empirical rovibrational energies for the V set.

The latest version of the MARVEL code, based on the MARVEL algorithm, is used to obtain empirical rotational–vibrational energy levels of $^{14}\text{N}_2^{16}\text{O}$, all characterized with well-defined uncertainties. The energies and the uncertainties of the V set are derived from a collection of previously measured [6,7,9,10,12,17,18,22–24,27,28,30–33,38,43,44,46,49,51,54–60,63,64,66–74,77,80–82,85,93,97,99–102,105,107,108,110,111,113,114,116,118–120,124,125,127–129,132–134,136,137,140–142,145,146,148,150,153,155–159,164,168–170,173–176,178] rotational–vibrational transitions with appropriate labels and uncertainties. Note that the uncertainties of the empirical energies reflect not only the accuracy of the individual measurements but also the topology of the SN; for example, how the most accurately determined transitions are connected.

2.2. Labeling

Low-lying vibrational states of semirigid molecules can be characterized using the standard harmonic oscillator (HO) notation [198]. In the case of the N_2O molecule, the standard way to denote the fundamentals is as follows: ν_1 (NO stretch), with a harmonic/anharmonic wavenumber of 1298/1285 cm^{-1} , ν_2 (degenerate bend), with wavenumbers close to 596/590 cm^{-1} , and ν_3 (NN stretch), at 2282/2224 cm^{-1} [83,190]. Upon excitation of the ν_2 mode, the bendings in the two, orthogonal planes can have different phases. Thus, an angular momentum arises as if the bent molecule rotated about the molecular axis. This so-called vibrational angular momentum quantum number, ℓ , takes positive values with $\ell = \nu_2, \nu_2 - 2, \nu_2 - 4, \dots$. Therefore, the vibrational states could be labeled as $(\nu_1 \nu_2^\ell \nu_3)$; thus, the label for the vibrational ground state is $(\nu_1 \nu_2^0 \nu_3) = (00^0 0)$.

The (harmonic and anharmonic) vibrational fundamentals obey the approximate relationship $\nu_3 \approx 2\nu_1 \approx 4\nu_2$. These relationships lead to many resonances among the excited vibrational states of $^{14}\text{N}_2^{16}\text{O}$,

meaning that they are best represented using a polyad notation $(P \ell N)$ [199,200], whereby the polyad number P is given by

$$P = 2\nu_1 + \nu_2 + 4\nu_3 \quad (1)$$

and N is the polyad counting number (the best way of defining N is discussed below). In addition, states with $\ell > 0$ can occur with both ‘e’ and ‘f’ rotationless parity, while those with $\ell = 0$ only correspond to ‘e’ states. Finally, all states are characterized by a total angular momentum quantum number, J , which has to satisfy $J \geq \ell$ for a given vibrational state. A surprising number of sources contained lines assigned to states with $J < \ell$. These lines were all removed from further analysis during the initial phase of our study.

Note that from this set of labels the only rigorous quantum numbers are J and the rotationless parity p ; these also give the total parity as $(-1)^{J+p}$, where $p = 0$ for ‘e’ states and 1 for ‘f’ states. In what follows, rovibrational states are labeled with the quintuplet $(P \ell N p J)$, with $p = \text{e/f}$.

While in principle it is straightforward to assign vibrational states to a given polyad, from about $P > 10$ the number of cases with significant interpolyad interactions [175,178] increases, which leads to resonances between states with different polyad numbers. Allocation of counting numbers N to vibrational states is also complicated. For states with $\ell = 0$ there is reasonable agreement in the literature about the appropriate counting numbers for particular vibrational bands. However, this is not true for states with $\ell > 0$, which show significant variation on the choice of N for the same state between different sources; these variations are particularly marked for states with $\ell = 2$.

In order to achieve a unique set of quantum numbers, required for the derivation of empirical energies via a MARVEL analysis, we adopted a two-step procedure. In order to be able to process the data successfully we grouped bands according to the stated band origins, adopting the value of N most commonly used in the literature. Once the complete transition set had been assembled and validated, we then renumbered all the polyads assuming that the lowest vibrational state for each (P, ℓ) combination was labeled $N = 1$, that states with $\ell \geq 1$ had a single band origin for the (quasi-)degenerate ‘e/f’ pair, and allowance was made for so-far unobserved vibrational levels. To get a master set we used the recent ‘Ames’ variational nuclear motion calculations of Huang et al. [177]. For this purpose we simply used the computed energy levels to give the lowest energy level for each vibrational band and then determined counting numbers from this list. The polyad number P for a given vibrational band, for which there were no disagreements between different experimental papers, were retained. This method avoided relying on quantum number assignments from either of the two variational nuclear motion calculations [177,201] we considered during this project; such assignments are also known to have difficulties for higher vibrational states and, indeed, the two studies do not always agree.

We note that these variational calculations do not actually give vibrational band origins for states with $\ell \geq 1$ as the $J = 0$ state is unphysical for these vibrational states; in this case we used the lowest ‘e’ level with $J = \ell$ for a given vibrational band. In practice, we found that the above procedure gave a canonical numbering scheme, which we provide below, without any significant problems or ambiguities. The full set of vibrational state labels with vibrational band origins and/or lowest state energies plus associated polyad and counting numbers are given in the Supplementary Material. We suggest that this numbering scheme should be adopted for future studies of the spectroscopy of N_2O .

2.3. Uncertainty quantification of energy levels: a bootstrap approach

It is important to transfer the (supposedly high) accuracy of high-resolution spectroscopic line-center measurement results to the empirical energy values derived through MARVEL. Due to issues one can legitimately raise with respect to the accuracy of many of the line uncertainties reported in experimental high-resolution spectroscopic

Table 1

Two examples illustrating how the bootstrap method applied works in determining uncertainties, with 95% confidence intervals, of empirical energy levels.

Energy level ($P \ell N e/f J$)	MARVEL energy / cm^{-1}	Original unc. / cm^{-1}	Bootstrap unc. / cm^{-1}	Tag of line	Initial unc. / cm^{-1}	Predicted energy / cm^{-1}
(17 1 14 e 36)	10 425.772	0.001	0.028	16KaCaKaPe.1421	0.001	10 425.772
				04BeCaPeTa.409	0.005	10 425.814
(16 2 10 e 25)	9374.588	0.001	0.022	22KaTaKaCab.2193	0.001	9374.588
				04BeCaPeTa.84	0.005	9374.635
				04BeCaPeTa.85	0.005	9374.634

investigations, the uncertainty associated with the empirical rovibrational energy levels must be determined with special care. There are cases where one can even question the true meaning of the uncertainty of an empirical energy level. In this study, we utilize a bootstrap method [202,203] to derive the final uncertainties of the empirical energy levels. In what follows we briefly explain why we switched from our previous best practice [204] to the bootstrap technique.

We have been testing various methods of generating uncertainties using the MARVEL procedure, including a robust method advocated by Watson [205], and the processing of transitions in segments, based on their claimed uncertainty [204] (this type of uncertainty is called here and later the *original* uncertainty). To obtain a self-consistent spectroscopic database, in all previous MARVEL-based studies it has proved necessary to manually increase the uncertainties of some of the measured transitions. Nevertheless, choosing the transitions for which the stated uncertainty needs to be increased is far from being straightforward. The principal reason for this is that the precision with which initial uncertainties are given by experimental spectroscopists can often be questioned. For example, it is easy to imagine cases where MARVEL leaves unchanged a relatively inaccurate measurement result because an overly-optimistic initial uncertainty was assigned to it and increases the uncertainty of a more accurate transition whose uncertainty was estimated pessimistically. As a result, even if several measurements are available the quantum state may become characterized by an incorrect energy value and an incorrect uncertainty. Unfortunately, without detailed knowledge of the measured spectra (actual spectra are very rarely published as supplementary material to spectroscopic papers), it is almost impossible to determine whether the initial uncertainties are optimistic or perhaps pessimistic; thus, this source of error is almost always present during a MARVEL-type joint analysis of the complete set of measured transitions. The only thing one can do is to increase the uncertainty of the energy levels where MARVEL has the chance, or even a tendency, to make an incorrect choice.

“Bootstrap” approaches [202,203] are suitable to obtain reasonable uncertainties in the case of conflicting measurements, where without this approach too small uncertainties would be given for energy levels if some of the measurement results were rejected. The variant of the bootstrap procedure we use is as follows: bootstrap samples are generated by multiplying the uncertainty of each transition by a random number between 1 and 10, and then we rerun MARVEL for each sample. After a hundred or more such runs, we check whether the average of the bootstrapped energies is different from the original MARVEL energy. If the energies calculated by the two methods differ by a prescribed amount, the uncertainty of the MARVEL energy is increased. If the energies calculated by the two methods are close but the standard deviation of the bootstrap energies is larger than the uncertainty of the original MARVEL energy, the uncertainty of the MARVEL energy will also be increased.

To illustrate how our version of the bootstrap method works, we present in Table 1 results for the two quantum states for which the ratio of the bootstrap uncertainty to the original uncertainty is the largest. The first quantum state, ($P \ell N e/f J$) = (17 1 14 e 36), is determined by two measured transitions, 16KaCaKaPe.1421 [150] and 04BeCaPeTa.409 [123]. The difference between the two predicted energy values is as large as 0.042 cm^{-1} , significantly larger than the reported experimental uncertainty of either line. Since the original

uncertainty of the supposedly more accurately measured transition is five times smaller than that of the other one, MARVEL increased the uncertainty of the second transition. However, without actually seeing the original spectra, it is impossible to decide whether the initial uncertainty of 16KaCaKaPe.1421 [150] is too optimistic or not. This line can be very weak, or saturated, or may also be subject to other measurement issues; therefore, based on the available experimental results the 0.001 cm^{-1} measurement uncertainty is too small. The bootstrap method detects the inconsistency between the predicted energy values and significantly increases the original uncertainty determined by MARVEL, reflecting better the present situation. In the second case, the energy of the (16 2 10 e 25) state is determined by three measured transitions coming from two sources [123,175]. Two of the transitions, coming from the same but older source, 04BeCaPeTa [123], predict the same empirical energy, but the third transition, with the smallest initial uncertainty from a very recent source, 22KaTaKaCab [175], predicts an energy value different by as much as 0.04 cm^{-1} . Thus, we are faced with the ‘philosophical’ question which measurements and which sources are more reliable. Unfortunately, without seeing the measured but unpublished spectra it is impossible to decide whether the stand-alone recent measurement, with lower uncertainty, or the transitions which are perceived to be less accurate but confirm each other are more accurate. If one were to accept the literature results, the lower-uncertainty choice would determine the energy value of the quantum state; therefore, MARVEL increased the uncertainties of the two other transitions. However, if the transition assumed to be the best is not as good as claimed by its ‘original’ uncertainty, we end up with an energy value with a much too small associated uncertainty. The bootstrap approach solves the dilemma by providing a significantly increased uncertainty for the energy level. Given the data available, this appears to be the better choice and the uncertainties reported in the Supplementary Material for the empirical energy levels were obtained with our version of the bootstrap technique.

3. Results and discussion

3.1. Data sources

During this study, a concerted effort was made to collate *all* measured and assigned rovibrational transitions of the $^{14}\text{N}_2^{16}\text{O}$ molecule available in the literature. The number of rovibrational transitions collected from the literature, based on 91 sources [6,7,9,10,12,17,22,27,30–33,38,43,44,46,49,51,54–60,63,64,66–74,77,80–82,85,93,97,99–102,105,107,108,110,111,113,114,116,118–120,123–125,127–129,132–134,136,140–142,145,146,148,150,153,155–159,164,168–170,173–176,178,180], is 67 930. We were able to validate 66 707 of these transitions via a detailed MARVEL-based analysis and a systematic check against the very recent variational nuclear motion calculations of Zobov et al. [201]. This check led to the removal of a small number of transitions which were inconsistent with these calculations. It is important to note that if a transition is not part of the principal component of the spectroscopic network of $^{14}\text{N}_2^{16}\text{O}$, we are not able to validate it. It is impressive that these experimental studies involved altogether 174 vibrational bands.

Some older sources, including 61RaWiRaEa [18], 64PITiMa [24], 64Pliva [23], and 68Plivaa [28], were considered insufficiently accurate to be included in the compilation of transitions data used during

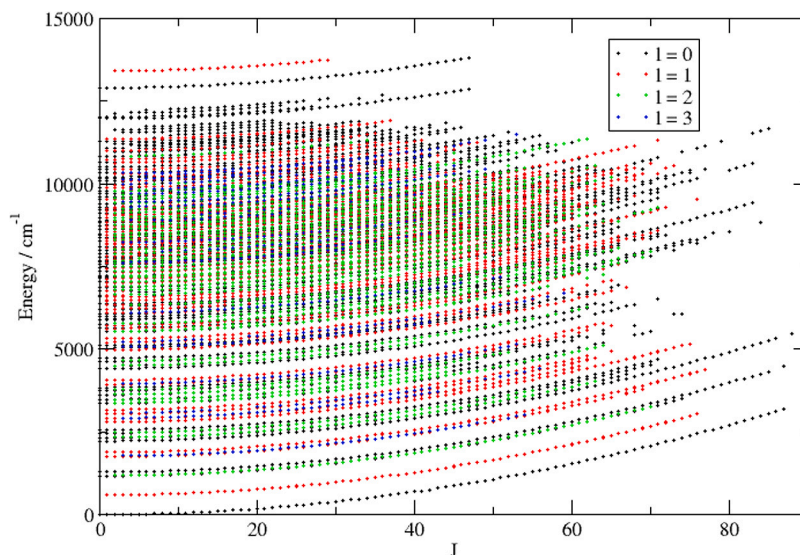


Fig. 1. Overview of the energy levels determined in this work designated by the ℓ and J quantum numbers.

the MARVEL analysis. We were unable to obtain a copy of the source 09SuDiZo [137].

Some of the older sources either explicitly mention that calibration is an issue, e.g., 50HeHe [7], or subsequent studies have identified the need for recalibration, e.g., for 82Guelachv [63]. Therefore, we tested a number of sources against the other available data to see which required recalibration. In the end, we recalibrated three data sets: the wavenumbers due to 50HeHe [7], 82Guelachv [63], and 95CaPeBaTe [93] were scaled by calibration factors of 0.99999811, 0.99999890, and of 1.00000308, respectively. Somewhat detailed notes on various sources are given in Appendix A to this paper.

The experimental sources used to construct the $^{14}\text{N}_2^{16}\text{O}$ spectroscopic network of this study are listed in Table 2. Table 2 also contains the information how many transitions have been validated and how many transitions we had to delete from each source (see the available(A) / validated(V) / deleted(D) column). The AOU (average original uncertainty) column shows the average of the measurement uncertainty of the given source and the values of AMR (average MARVEL reproduction) shows how well, in an average sense, the empirical (MARVEL) energy levels are able to reproduce the experimentally measured lines of the given source. The last column of Table 2, MR, shows the maximum reproduction of the given source, i.e., the largest difference between the experimentally measured wavenumber and the transition predicted by MARVEL. For most sources all measured transitions have been validated. Nevertheless, we did identify a number of incompatibilities in between some of the sources, which led us to delete a number of lines. The largest number of deleted transitions, 121, 112, and 88 concern the sources 60TiPIBe [17], 06HePiGuSo [128], and 50HeHe [7], respectively. It is noteworthy that for 60TiPIBe [17] this means that almost one fourth of the measured lines in the infrared region had to be deleted.

The SN of $^{14}\text{N}_2^{16}\text{O}$ has a single principal component. This is due to the rigidity of the NN unit. Altogether, out of the 67930 transitions considered, we could validate 66707, all belonging to the principal component. 635 transitions, which should belong to the principal component, were removed during our MARVEL analysis. While some of these transitions have been misassignments (or have $J < \ell$), most were removed on the ground of accuracy. The remaining 616 transitions belong to 167 floating components; we did not make an attempt to attach these to the principal component of the SN of $^{14}\text{N}_2^{16}\text{O}$. It is also worth emphasizing that among the 67930 transitions considered there are only 43246 unique ones. This means that a significant number of transitions have been measured more than once; in fact, the number

of transitions measured just one time is 27444, while there are 4 and 142 transitions which were measured 7 and 6 times, respectively (the number of empirical rovibrational energy levels determined, 17561, is significantly closer to 43000 than to 68000).

Note also that in SNs the degrees of the energy levels display an inverse-power-law-like distribution [194,195], implying the presence of a small number of high-degree quantum states, called hubs, in the SN. The highest-degree hubs of $^{14}\text{N}_2^{16}\text{O}$ have the general label (0 0 1 e J) with $J = 11, 12, 13, 15, 16, 17$, and 18, and these vertices have as many as 500 connecting edges each. This means that if hubs are defined as the top 1% of the vertices with the highest degrees (this translates to 174 hubs for the present dataset), than slightly more than 60% of the transitions are connected to less than 1% of the vertices (apart from a diminishing number of exceptions, hubs are the lower states of the measured transitions). These observations are of interest especially for future high-resolution and precision-spectroscopy experiments, including those aiming at the presently readily available accuracy of a few kHz [206–208] rather than several MHz.

Fig. 1 shows the distribution of the 17561 empirical energy levels determined as a function of the J rotational quantum number. To provide additional information, the states with different ℓ values are indicated with different colors. As seen in Fig. 1, our network includes levels with $\ell \leq 3$. In practice, 01BaVe [113] and 22KaTaKaCaa [174] contain a combined total of 223 transitions to states with $\ell = 4$ and 01BaVe [113] gives 224 transitions to states with $\ell = 5$, meaning that all but two of the transitions not attached to the principal component are associated with states with $\ell > 3$.

3.2. Level uncertainties

As mentioned in Section 2.3, in this study we employed a method new to MARVEL, called bootstrap, which does not alter the uncertainties of the measured transitions but improves the uncertainties of the empirical (MARVEL) energy levels. The bootstrap approach applied can only increase the uncertainties.

Fig. 2 shows the ratio of the ‘bootstrap’ and the ‘original’ uncertainties of the empirical rovibrational energy levels. In most cases, the bootstrap algorithm barely raises the original MARVEL uncertainties. In 92% of cases the ratio is less than 5 and in only 1.5% of cases the ratio is larger than 10. These numbers suggest that the ‘original’ uncertainty estimation employed within MARVEL is a good approximation in most cases, but in about 1-2% of the cases it is necessary to increase the uncertainty of the empirical energy levels significantly. The ratio above

Table 2

Experimental sources used to construct the $^{14}\text{N}_2^{16}\text{O}$ rovibrational spectroscopic network of this study. The data given include, for each source, the wavenumber ranges of the validated transitions (in cm^{-1}), the number of actual (*A*), validated (*V*), and deleted (*D*) transitions, and selected uncertainty statistics (in cm^{-1}), where *AOU* = average original uncertainty, *AMR* = average MARVEL reproduction of the source's lines, and *MR* = maximum reproduction in the source. RC (in the tag) = recalibrated source (see text).

Segment tag	Range	A/V/D	AIU	AMR	MR
78ReMeDy [58]	0.002–0.009	3/3/0	5.00×10^{-9}	1.10×10^{-12}	5.00×10^{-9}
64LaLi [22]	0.835–2.521	4/4/0	2.67×10^{-6}	3.60×10^{-7}	3.34×10^{-6}
47CoElGo [6]	0.838–0.838	1/1/0	3.34×10^{-6}	1.34×10^{-7}	3.34×10^{-6}
75CaKu [51]	0.838–0.838	1/1/0	2.07×10^{-8}	2.40×10^{-11}	2.07×10^{-8}
75Bogey [49]	1.662–4.156	4/4/0	4.59×10^{-6}	2.84×10^{-6}	8.34×10^{-6}
52Tetenbau [10]	1.676–1.676	1/1/0	3.34×10^{-6}	1.20×10^{-5}	1.20×10^{-5}
70ScMuLa [32]	1.676–2.514	2/2/0	3.50×10^{-7}	7.34×10^{-9}	4.34×10^{-7}
71LeHoThMa [33]	2.504–2.519	5/4/1	3.34×10^{-6}	3.87×10^{-7}	3.34×10^{-6}
51JoTrGo [9]	3.352–4.190	2/2/0	9.17×10^{-6}	1.07×10^{-6}	1.00×10^{-5}
56BuGo [12]	3.352–10.055	9/9/0	1.33×10^{-5}	5.45×10^{-6}	2.00×10^{-5}
70PeSuFr [30]	4.172–10.082	35/34/1	2.64×10^{-6}	1.50×10^{-6}	1.60×10^{-5}
18LaScAgMe [157]	5.028–5.866	2/2/0	4.00×10^{-6}	2.60×10^{-6}	4.36×10^{-6}
68FrAr [27]	5.028–5.028	1/1/0	6.67×10^{-6}	1.83×10^{-6}	6.67×10^{-6}
14TiChChCh [146]	6.676–2272.183	219/212/0	1.17×10^{-6}	2.03×10^{-7}	1.01×10^{-5}
74BuVaGeKa [43]	10.055–15.918	6/6/0	1.67×10^{-6}	3.62×10^{-7}	1.67×10^{-6}
76AnBuKaKr [56]	12.568–18.518	97/97/0	7.50×10^{-7}	8.04×10^{-8}	3.04×10^{-6}
06DrMa [127]	20.103–55.230	72/71/0	2.50×10^{-6}	6.81×10^{-7}	7.58×10^{-6}
90Yamada [82]	20.103–47.637	32/32/0	1.00×10^{-4}	7.18×10^{-5}	1.64×10^{-4}
03MoYa [120]	20.940–21.776	2/2/0	5.00×10^{-8}	2.05×10^{-9}	5.34×10^{-8}
97MoFaTaYa [102]	20.940–24.285	5/5/0	6.67×10^{-7}	1.40×10^{-6}	1.78×10^{-6}
99MoYaMa [108]	20.862–26.081	60/60/0	6.87×10^{-7}	2.41×10^{-7}	5.80×10^{-6}
89VaJeWeMa [80]	50.129–50.241	3/3/0	6.67×10^{-6}	7.52×10^{-7}	6.67×10^{-6}
83JoKaHo [64]	542.456–645.418	355/355/0	4.00×10^{-5}	1.28×10^{-4}	6.79×10^{-4}
07Horneman [132]	542.920–635.235	533/509/24	1.74×10^{-5}	2.26×10^{-5}	2.26×10^{-3}
92TaLoLu [85]	554.029–619.385	241/241/0	5.00×10^{-5}	1.01×10^{-4}	1.20×10^{-3}
96WeSiRe [101]	557.231–615.994	96/96/0	6.00×10^{-4}	1.27×10^{-4}	6.00×10^{-4}
04Toth [125]	577.760–7232.274	1121/1121/0	5.00×10^{-4}	1.25×10^{-4}	3.33×10^{-3}
89MaWeVa [77]	896.945–989.668	18/18/0	1.74×10^{-4}	6.89×10^{-5}	3.34×10^{-4}
96TaEvZiMa [100]	897.010–1074.417	129/129/0	1.67×10^{-7}	9.99×10^{-8}	2.22×10^{-6}
87Toth [73]	900.926–2392.452	1207/1196/0	6.00×10^{-5}	3.27×10^{-5}	9.44×10^{-4}
72SoJa [38]	922.423–956.347	27/27/0	1.95×10^{-4}	9.13×10^{-4}	1.12×10^{-3}
75WhSuRiHa [54]	925.982–970.092	33/33/0	8.34×10^{-7}	1.45×10^{-6}	3.80×10^{-6}
87ZiWeMa [74]	1037.189–1084.591	9/9/0	1.59×10^{-4}	4.86×10^{-5}	2.67×10^{-4}
85WeJeHiMu [70]	1104.849–1914.718	32/31/0	2.81×10^{-4}	1.63×10^{-4}	7.98×10^{-4}
86Toth [71]	1104.791–1348.351	1061/1047/0	6.00×10^{-5}	4.40×10^{-5}	6.46×10^{-4}
82Guelachv_RC [63]	1118.129–1342.938	649/649/0	5.00×10^{-5}	1.10×10^{-4}	9.99×10^{-4}
84Toth [67]	1133.468–1236.586	54/54/0	2.00×10^{-4}	2.80×10^{-4}	7.83×10^{-4}
85BrTo [68]	1132.024–4749.125	240/240/0	6.00×10^{-5}	5.93×10^{-5}	2.58×10^{-4}
15GaCaCoFa [148]	1161.479–1161.479	1/1/0	3.00×10^{-7}	1.49×10^{-7}	3.00×10^{-7}
18AlLaGala [156]	1245.765–1309.847	73/73/0	2.69×10^{-5}	8.41×10^{-6}	1.36×10^{-4}
21HjGeKrHu [168]	1251.600–1318.138	179/179/0	8.07×10^{-6}	5.67×10^{-6}	2.39×10^{-4}
85WeHiMa [69]	1257.316–1339.843	14/14/0	1.57×10^{-4}	1.24×10^{-4}	4.65×10^{-4}
87HiWeMa [72]	1257.509–1335.006	28/24/4	1.69×10^{-4}	1.97×10^{-4}	1.97×10^{-3}
80NaKaYaHa [60]	1295.476–1311.284	4/4/0	5.25×10^{-4}	4.77×10^{-4}	9.13×10^{-4}
89VaScWeMa [81]	1591.326–1672.707	8/8/0	2.59×10^{-4}	1.21×10^{-4}	3.34×10^{-4}
76AmGu [55]	1831.706–3191.180	3944/3861/77	2.00×10^{-4}	3.81×10^{-4}	5.59×10^{-3}
01BaVe [113]	2044.525–2266.349	3242/3071/7	8.00×10^{-3}	7.27×10^{-4}	6.75×10^{-2}
03BaPiVe [118]	2072.675–2200.925	753/444/1	4.00×10^{-4}	2.46×10^{-4}	3.09×10^{-3}
74FaDu [44]	2098.489–2230.678	997/994/3	3.00×10^{-3}	3.97×10^{-3}	4.07×10^{-2}
76VaLeCaBo [57]	2135.289–2268.099	201/134/67	5.00×10^{-4}	8.89×10^{-4}	8.10×10^{-3}
13KnWiGiRa [145]	2189.273–2213.246	24/24/0	2.67×10^{-5}	1.47×10^{-5}	4.02×10^{-5}
21JiMc [169]	2206.659–2208.093	3/3/0	2.00×10^{-4}	1.39×10^{-5}	2.00×10^{-4}
04NeSuVa [124]	2224.588–2251.574	38/38/0	5.00×10^{-4}	6.92×10^{-5}	5.00×10^{-4}
74KrSa [46]	2267.096–2618.035	1838/1825/13	2.00×10^{-2}	3.22×10^{-3}	5.00×10^{-2}
60TiPiBe [17]	2438.220–3502.620	884/763/121	5.10×10^{-2}	3.03×10^{-2}	1.64×10^{-1}
99Toth [110]	3676.940–7795.203	1328/1328/0	2.78×10^{-4}	5.43×10^{-5}	4.49×10^{-3}
06HePiGuSo [128]	3900.809–4041.312	1011/893/112	1.00×10^{-3}	6.19×10^{-4}	1.50×10^{-2}
84PoPeJeWe [66]	4341.141–4753.311	39/39/0	1.97×10^{-4}	5.79×10^{-5}	4.00×10^{-4}
16WeBrSeWe [153]	4418.202–4439.792	41/41/0	4.66×10^{-5}	3.55×10^{-4}	4.29×10^{-4}
20ZhBaFlHo [164]	4415.014–4415.014	1/1/0	2.00×10^{-5}	4.83×10^{-6}	2.00×10^{-5}
80BrCoCuHo [59]	4607.694–4657.886	64/64/0	1.00×10^{-3}	8.71×10^{-4}	1.48×10^{-3}
06WaPeTaGa [129]	5313.693–8987.678	2356/2356/0	5.96×10^{-3}	3.76×10^{-3}	3.13×10^{-2}
19BeMoKaKa [158]	5696.223–5908.020	2166/2166/0	1.11×10^{-3}	5.65×10^{-4}	3.24×10^{-2}
07LiKaPeTa [134]	5906.331–6832.402	2217/2213/4	1.00×10^{-3}	9.73×10^{-4}	1.76×10^{-2}
07LiKaMaRo [133]	6001.771–6884.882	5094/5072/1	1.42×10^{-3}	1.01×10^{-3}	3.08×10^{-2}
00WeKaCaBa [111]	6436.315–12141.237	3578/3538/40	2.69×10^{-3}	4.39×10^{-3}	6.51×10^{-2}
95CaPeBaTe_RC [93]	6436.313–10832.947	3160/3158/2	5.00×10^{-3}	4.43×10^{-3}	8.92×10^{-2}
19LiWaTaKa [159]	6519.115–6597.240	88/88/0	8.86×10^{-6}	4.21×10^{-6}	5.44×10^{-5}
22Iwakuni [173]	6549.562–6596.114	46/46/0	1.83×10^{-5}	1.40×10^{-5}	8.87×10^{-5}
09LiKaPeHu [136]	6789.852–7065.586	1154/1148/6	1.00×10^{-3}	1.11×10^{-3}	2.21×10^{-2}
12LuMoLiPe [142]	6949.767–7725.398	6226/6191/12	1.00×10^{-3}	6.69×10^{-4}	1.33×10^{-2}
23KaMoTaCa [178]	7250.027–7652.630	3329/3307/0	1.00×10^{-3}	6.11×10^{-4}	3.60×10^{-2}
16KaCaKaPe [150]	7601.172–8329.631	2968/2963/5	1.00×10^{-3}	5.88×10^{-4}	2.72×10^{-2}

(continued on next page)

Table 2 (continued).

11LiKaPeTa [140]	7647.529–7918.173	1746/1742/4	1.00×10^{-3}	9.13×10^{-4}	2.42×10^{-2}
22KaTaKaCab [175]	7647.527–7988.178	2423/2421/2	1.00×10^{-3}	6.57×10^{-4}	2.36×10^{-2}
99HiQu [107]	7783.475–7788.489	8/8/0	1.00×10^{-3}	1.17×10^{-3}	2.03×10^{-3}
50HeHe_RC [7]	7970.763–12898.443	1148/1060/88	3.00×10^{-2}	3.19×10^{-2}	1.51×10^{-1}
22KaTaKaCaa [174]	8272.503–8619.558	3132/3097/3	8.00×10^{-4}	4.07×10^{-4}	1.66×10^{-2}
21KaKaTaCa [170]	8325.774–8622.078	2745/2745/0	1.00×10^{-3}	5.51×10^{-4}	1.66×10^{-2}
03DiPeTaTe [119]	8836.109–10092.626	719/692/27	3.23×10^{-3}	5.12×10^{-3}	3.44×10^{-2}
04BeCaPeTa [123]	9074.119–9621.037	659/658/1	5.10×10^{-3}	4.55×10^{-3}	5.27×10^{-2}
98GaCaKaSt [105]	9362.110–9419.797	68/68/0	5.37×10^{-3}	1.90×10^{-2}	4.68×10^{-2}
24SiSeEmMa [180]	9842.540–11972.969	235/231/4	4.51×10^{-4}	1.34×10^{-3}	1.48×10^{-2}
02BeKaCa [116]	9910.657–9951.791	22/22/0	1.00×10^{-2}	5.79×10^{-3}	2.45×10^{-2}
01CaWeTaPe [114]	10084.048–12021.132	946/943/3	1.76×10^{-2}	5.09×10^{-3}	9.63×10^{-2}
70Pliva [31]	10756.448–10832.966	134/134/0	1.50×10^{-2}	3.81×10^{-3}	1.64×10^{-2}
22LuGo [176]	11233.770–11283.200	53/53/0	1.02×10^{-2}	8.08×10^{-3}	3.85×10^{-2}
96Campargu [97]	11233.777–12221.945	241/241/0	1.50×10^{-2}	9.71×10^{-3}	6.06×10^{-2}
11MiPeTaCa [141]	12764.164–12899.183	140/140/0	1.00×10^{-2}	4.81×10^{-3}	3.31×10^{-2}
17ZhWaLiZh [155]	12857.786–12898.904	41/41/0	2.82×10^{-3}	6.14×10^{-4}	6.42×10^{-3}

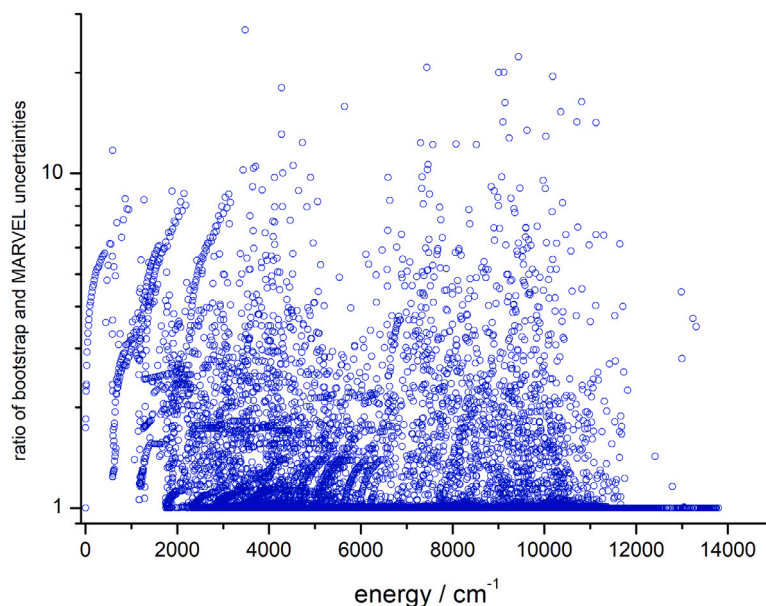


Fig. 2. Ratio of the uncertainties of the empirical rovibrational energy levels of the new bootstrap approach and the traditional MARVEL estimates.

about 12000 cm^{-1} is almost always one. This is due to the fact that the bootstrap approach will only increase the uncertainty if there are more than one (conflicting) measurements available.

3.3. Vibrational bands and band origins

Table 3 summarizes the vibrational bands which could be determined based on the set of measured rovibrational transitions. It is important to note that we use the $\ell = J$ definition for a vibrational band origin (VBO), *i.e.*, where $\ell > 0$, we treat the lowest possible energy level as the VBO. While comparing the 78 VBOs (with $P_{\max} = 24$) determined through our MARVEL analysis to effective Hamiltonian parameters of 04Toth [125], for the $(P \ell N) = (111)$ VBO we observed a significant discrepancy. Since this VBO is determined in our MARVEL analysis by a single measured transition, taken from 50HeHe [7], and the uncertainty of this band is 0.06 cm^{-1} , we finally did not delete this transition but issue this warning. Future accurate measurements should be able to settle this simple issue.

There are a further number of small but significant discrepancies among the entries of Table 3, on the order of 0.001 cm^{-1} , not discussed here. It is worth pointing out the discrepancies larger than 0.01 cm^{-1} . Such cases include $(P \ell N) = (1117)$, (1226) , (1317) , (1519) , and (17315) . For $P > 19$ there are significant discrepancies for most states. These deviations require further detailed studies, beyond the scope of the present investigation.

3.4. Empirical rovibrational energy levels

From the 67 930 measured rovibrational transitions (43 246 unique ones) collected we were able to determine 17 561 energy levels from 0 up to 13790 cm^{-1} . The highest rotational quantum number, J , in our empirical (MARVEL) energy-level set is 88, being part of the $(P \ell N) = (401)$ vibrational band. The largest polyad number, P , and polyad counting number, N , are 25 and 28, respectively. We note that 200GmMuMu [165] used a novel optical centrifuge technique to measure transitions involving rotational states up to $J = 206$; however, they only actually measured 11 between $J'' = 140$ and $J'' = 205$, so these data could not be used to form a network. The vibrational excitations v_1 , v_2 , and v_3 range up to 9, 16, and 5, respectively.

We note that coverage of the states with $\ell = 0, 1$, and 2 generally extends to high energy (polyad number). The coverage is more limited for states with $\ell = 3$. While a few transitions involving levels with $\ell = 4$ and 5 have been observed (*vide supra*), these do not connect to the principal component; thus, the empirical energy levels we have determined are limited to those with $\ell \leq 3$.

4. Comparison with previous line lists

This section provides comparisons of our MARVEL-based results with two line lists, namely the SISAM database, called here 04Toth [125], and the very recent Nitrous Oxide Spectroscopic Line List (NOSL-296) [179], designed for atmospheric applications.

Table 3

Summary of the vibrational states of $^{14}\text{N}_2^{16}\text{O}$ considered in this work. The vibrational states are designated using the polyad-based notation (P, ℓ, N), with $P = 2v_1 + v_2 + 4v_3$, and ℓ and N are the vibrational angular momentum quantum number and the polyad counting number, respectively. The lowest, $J = \ell$, energy level for each vibrational band given by the calculations of Huang et al. [177], denoted Ames, and the empirical, effective Hamiltonian (EH) band origins (with citations), are given in cm^{-1} .

$P \ell N$	MARVEL	AMES	EH	$P \ell N$	MARVEL	AMES	EH	$P \ell N$	MARVEL	AMES	EH
0 0 1	0.0(0)	0.00	0.000 [125]	11 1 8	6571.590(1)	6571.60	6571.590 [125]	15 1 5	8425.849(1)	8425.75	8425.847 [175]
1 1 1	589.606223(7)	589.60	589.606 [125]	11 1 9	6631.431(2)	6631.77	6631.429 [133]	15 1 8	8560.0019(8)	8560.05	8560.000 [129]
2 0 1	1168.13237(2)	1168.13	1168.132 [125]	11 1 10	6773.346(7)	6773.61	6773.348 [134]	15 1 9	8666.974(2)	8667.05	8666.938 [150]
2 0 2	1284.903342(5)	1284.91	1284.903 [125]	11 1 11	6893.051(2)	6893.21	6893.051 [133]	15 1 10	8705.236(1)	8705.82	8702.237 [150]
2 2 1	1180.26532(2)	1180.26	1180.265 [125]	11 1 12	6996.842(2)	6996.94	6996.840 [133]	15 1 11	8708.369(1)	8709.61	8705.366 [150]
3 1 1	1749.9042(4)	1749.90	1749.907 [125]	12 0 1	6580.85352(1)	6580.82	6580.854 [125]	15 1 12	8844.271(1)	8844.56	8844.278 [142]
3 1 2	1881.1003(2)	1881.12	1881.101 [125]	12 0 2	6630.434(2)	6630.39	6630.429 [134]	15 1 14	8960.5835(8)	8960.75	8960.588 [150]
3 3 1	1771.9597(3)	1771.97	1771.960 [125]	12 0 4	6768.502(1)	6768.45	6768.502 [125]	15 1 16	9062.1621(8)	9062.26	9062.158 [142]
4 0 1	2223.7567419(3)	2223.76	2223.757 [125]	12 0 6	6868.5498(2)	6868.52	6868.550 [125]	15 1 17	9186.5218(8)	9187.96	9186.521 [178]
4 0 2	2322.57323(6)	2322.56	2322.573 [125]	12 0 7	6882.691(1)	6882.61	6882.692 [158]	15 3 1	8225.739(2)	8225.72	8225.737 [133]
4 0 3	2461.9965(2)	2462.03	2461.996 [125]	12 0 8	7024.091(1)	7024.10	7024.093 [142]	16 0 1	8714.1402(4)	8714.09	8714.139 [133]
4 0 4	2563.3403(2)	2563.32	2563.339 [125]	12 0 9	7029.844(1)	7030.51	7029.843 [142]	16 0 4	8877.042(1)	8877.02	8877.040 [142]
4 2 1	2333.64607(6)	2333.65	2333.646 [125]	12 0 10	7137.127(1)	7137.09	7137.127 [125]	16 0 7	8976.489(1)	8976.47	8976.488 [142]
4 2 2	2477.3089(2)	2477.33	2477.310 [125]	12 0 11	7194.365(1)	7194.95	7194.365 [134]	16 0 10	9108.322(3)	9108.34	9108.323 [150]
5 1 1	2799.1245(2)	2799.13	2799.124 [125]	12 0 12	7214.680(1)	7214.68	7214.680 [125]	16 0 11	9219.056(1)	9218.99	9219.056 [150]
5 1 2	2898.65323(6)	2898.65	2898.657 [125]	12 0 13	7340.792(1)	7341.29	7340.792 [134]	16 0 14	9294.994(1)	9294.98	9294.993 [150]
5 1 3	3047.0490(2)	3047.07	3047.048 [125]	12 0 14	7463.985(1)	7464.32	7463.986 [133]	16 0 15	9398.818(1)	9399.25	9398.817 [150]
5 1 4	3166.68(2)	3166.68	3166.685 [125]	12 0 15	7556.136(1)	7556.36	7556.135 [133]	16 0 17	9517.874(8)	9518.10	9517.874 [150]
5 3 1	2919.0973(3)	2919.12	2919.098 [125]	12 0 16	7640.474(1)	7640.67	7640.476 [133]	16 0 18	9599.1039(8)	9601.02	9599.103 [174]
6 0 1	3363.9780(2)	3363.98	3363.978 [125]	12 2 1	6640.670(1)	6640.66	6640.667 [134]	16 0 19	9606.336(5)	9606.34	9606.332 [150]
6 0 2	3466.60018(6)	3466.62	3466.600 [125]	12 2 3	6782.826(2)	6782.81	6782.825 [134]	16 0 20	9690.0821(8)	9690.13	9690.082 [170]
6 0 3	3480.81930(6)	3480.82	3480.819 [125]	12 2 5	6894.268(2)	6894.22	6894.268 [158]	16 0 22	9874.2970(8)	9875.91	9874.296 [170]
6 0 4	3620.9430(2)	3620.92	3620.943 [125]	12 2 6	7039.494(2)	7039.73	7039.491 [152]	16 2 2	8749.056(1)	8749.07	8749.056 [133]
6 0 5	3748.2521(2)	3748.25	3748.252 [125]	12 2 7	7040.686(2)	7041.19	7040.685 [142]	16 2 4	8890.970(1)	8891.06	8890.970 [142]
6 0 6	3836.37100(3)	3836.35	3836.371 [125]	12 2 9	7207.024(1)	7207.62	7207.022 [134]	16 2 6	8980.053(1)	8979.95	8980.051 [175]
6 2 1	3375.6413(2)	3375.64	3375.642 [125]	12 2 10	7357.528(2)	7358.04	7357.528 [133]	16 2 7	9123.706(1)	9082.03	9123.706 [150]
6 2 2	3476.97731(6)	3477.01	3476.978 [125]	12 2 11	7491.112(2)	7491.48	7491.112 [133]	16 2 7	9123.706(1)	9123.85	9123.706 [150]
6 2 3	3634.1032(2)	3634.08	3634.104 [125]	12 2 12	7613.096(2)	7613.23	7613.096 [133]	16 2 11	9415.442(1)	9415.97	9415.442 [170]
6 2 4	3768.5551(2)	3768.55	3768.555 [125]	13 1 1	7127.798(1)	7127.77	7127.798 [125]	16 2 13	9545.384(1)	9545.79	9545.384 [150]
7 1 1	3932.0805(6)	3932.08	3932.083 [125]	13 1 7	7443.822(1)	7443.85	7443.746 [134]	16 2 16	9763.7896(8)	9765.71	9763.790 [174]
7 1 3	4062.8091(4)	4062.80	4062.809 [125]	13 1 8	7590.240(1)	7590.39	7590.244 [142]	17 1 1	9246.894(1)	9246.87	9246.893 [142]
7 3 1	3953.2921(2)	3953.29	3953.293 [125]	13 1 10	7715.885(2)	7715.96	7715.886 [134]	17 1 7	9538.070(5)	9538.21	9538.065 [142]
8 0 1	4417.37778(3)	4417.37	4417.378 [125]	13 1 12	7818.651(2)	7818.72	7818.650 [134]	17 1 14	9885.506(1)	9885.65	9885.509 [150]
8 0 4	4630.1613(2)	4630.14	4630.161 [125]	13 1 14	8047.173(1)	8047.85	8047.178 [134]	17 3 4	9445.920(1)	9446.11	9445.919 [142]
8 0 5	4730.82507(3)	4730.81	4730.825 [125]	13 1 15	8160.484(1)	8160.97	8160.484 [134]	17 3 14	9988.527(1)	9989.36	9988.522 [150]
8 0 8	5026.30302(3)	5026.27	5026.303 [125]	13 1 16	8267.106(1)	8268.17	8267.108 [133]	17 3 15	10112.1369(8)	10106.90	10106.360 [170]
8 0 9	5105.67692(3)	5105.68	5105.677 [125]	13 3 7	7618.257(2)	7618.39	7618.257 [158]	18 0 1	9770.6360(8)	9770.61	9770.636 [170]
8 2 1	4502.1990(4)	4502.21	4502.199 [125]	14 0 1	7665.273(1)	7665.21	7665.273 [133]	18 0 7	10079.556(3)	10079.59	10079.565 [175]
9 1 1	4978.526(3)	4978.51	4978.524 [125]	14 0 3	7782.662(1)	7782.65	7782.662 [125]	18 0 8	10163.593(1)	10163.56	10163.598 [114]
9 1 4	5201.61(2)	5201.59	5201.613 [125]	14 0 5	7874.156(1)	7874.08	7874.156 [134]	18 0 12	10204.80(2)	10204.81	10204.806 [114]
9 1 5	5319.96(3)	5319.98	5320.001 [125]	14 0 8	7998.589(2)	7998.57	7998.585 [134]	18 0 13	10332.02(2)	10332.06	10332.013 [114]
9 1 8	5618.60187(3)	5618.60	5618.597 [125]	14 0 9	8083.953(1)	8083.91	8083.955 [134]	18 0 16	10429.15(2)	10428.98	10429.148 [114]
9 1 9	5723.651(1)	5723.66	5723.653 [125]	14 0 12	8276.326(1)	8276.44	8276.325 [142]	18 0 17	10504.41(3)	10504.45	10504.398 [114]
9 3 1	5074.0908(5)	5074.12	5074.091 [125]	14 0 14	8376.3502(8)	8376.32	8376.350 [142]	18 0 20	10640.61(2)	10641.28	10640.611 [114]
9 3 3	5227.459(1)	5227.44	5227.460 [125]	14 0 15	8452.6357(8)	8452.70	8452.636 [142]	18 2 1	9781.143(1)	9781.15	9781.143 [170]
10 0 3	5646.74022(3)	5646.73	5646.740 [125]	14 0 16	8475.7282(8)	8475.87	8475.724 [142]	19 1 10	10733.302(1)	10733.53	10733.308 [114]
10 0 5	5762.372(1)	5762.31	5762.373 [125]	14 0 17	8612.948(1)	8613.96	8612.949 [142]	19 1 17	11000.56(2)	11000.67	11000.160 [114]
10 0 7	5902.968(2)	5903.19	5902.966 [134]	14 0 18	8725.101(1)	8725.10	8725.100 [142]	19 3 1	10316.845(1)	10316.93	10316.848 [174]
10 0 8	5974.84501(3)	5974.81	5974.845 [125]	14 0 19	8810.765(1)	8811.42	8810.762 [142]	20 0 1	10815.251(5)	10815.24	10815.242 [170]
10 0 9	6058.668(2)	6058.81	6058.667 [125]	14 2 1	7676.0959(6)	7676.06	7676.095 [133]	20 0 2	10820.128(5)	10820.14	10820.122 [114]
10 0 10	6192.270(2)	6192.35	6192.271 [125]	14 2 4	7886.494(1)	7886.49	7886.494 [134]	20 0 11	11271.99(2)	11271.99	11271.998 [114]
10 0 12	6373.308(2)	6373.38	6373.308 [125]	14 2 7	8017.943(1)	8018.03	8017.945 [134]	21 1 1	11334.685(5)	11334.79	11334.289 [111]
10 2 1	5540.9177(4)	5540.89	5540.917 [125]	14 2 10	8296.81	8296.81	8296.81 [142]	22 0 4	11964.12(6)	11964.36	11964.252 [114]
10 2 4	5775.118(1)	5775.09	5775.118 [125]	14 2 12	8417.273(2)	8417.43	8417.273 [142]	22 0 5	12009.05(2)	12009.20	12009.029 [114]
11 1 1	6084.143(2)	6084.12	6084.143 [134]	14 2 13	8490.353(1)	8491.53	8490.353 [142]	24 0 2	12891.079(5)	12891.09	12891.153 [114]
11 1 3	6214.638(2)	6214.62	6214.640 [125]	14 2 14	8633.615(1)	8634.68	8633.614 [142]				
11 1 5	6327.090(1)	6327.02	6327.312 [142]	14 2 15	8762.569(1)	8763.39	8762.570 [142]				
11 1 6	6462.895(2)	6462.90	6462.898 [125]	15 1 1	8206.086(1)	8206.07	8206.090 [133]				
11 1 7	6470.361(1)	6470.80	6467.371 [158]	15 1 3	8336.6118(8)	8336.64	8336.611 [133]				

4.1. O4Toth [125]

The SISAM database contains 32 637 $^{14}\text{N}_2^{16}\text{O}$ rovibrational lines and covers the 525 – 7797 cm^{-1} wavenumber region. While most of these transitions were generated using effective Hamiltonians, the original measured values were retained for those transitions identified as being significantly perturbed by resonances. As a result, 1164 transitions from the SISAM data were identified as observed rather than calculated. Inspection showed that 43 of these transitions were provided by previous measurements by Toth [71,73,110]; thus, 1121 transitions were added to our compilation. An uncertainty of 0.000 5 cm^{-1} was used for these transitions, based on self-consistency with other transitions in our dataset.

We used the effective Hamiltonian parameters of O4Toth [125] to check our MARVEL energy levels. Results of this comparison can be seen in Fig. 3. Almost all of the differences are smaller than 0.01 cm^{-1} ; the deviations are larger than 0.01 cm^{-1} only for relatively high J values ($J > 50$). We checked how many experimental measurements determine those MARVEL energy levels that have large difference from the O4Toth values and it turned out that most of them are determined by only one or two measurements (see the red squares in Fig. 3).

While MARVEL levels determined by a single measurement must be regarded as less trustworthy, it is likely that the issue here was with poor extrapolation of the effective Hamiltonian used by O4Toth.

4.2. NOSL-296 [179]

The NOSL-296 line list [179] contains almost 900 000 lines, covering the 0.02 – 13 378 cm^{-1} wavenumber range. The authors published neither the values of the effective Hamiltonian parameters nor those of the energy levels; therefore, to make a meaningful comparison, we had to calculate them. Using the energy value of the lower quantum state of the transition, given in the line list, and values of the wavenumber entries, we could determine 67 028 rovibrational energy levels. During the comparison of these data with those of the present study, we identified an issue: there are significant differences between the measurements of 23KaMoTaCa [178] and the NOSL-296 [179] line positions. The Supplementary Material of 23KaMoTaCa [178] has indicated the presence of such differences. Therefore, we divided our comparison into two parts: (a) first we checked those MARVEL energy levels that are determined by at least three measured lines (see the

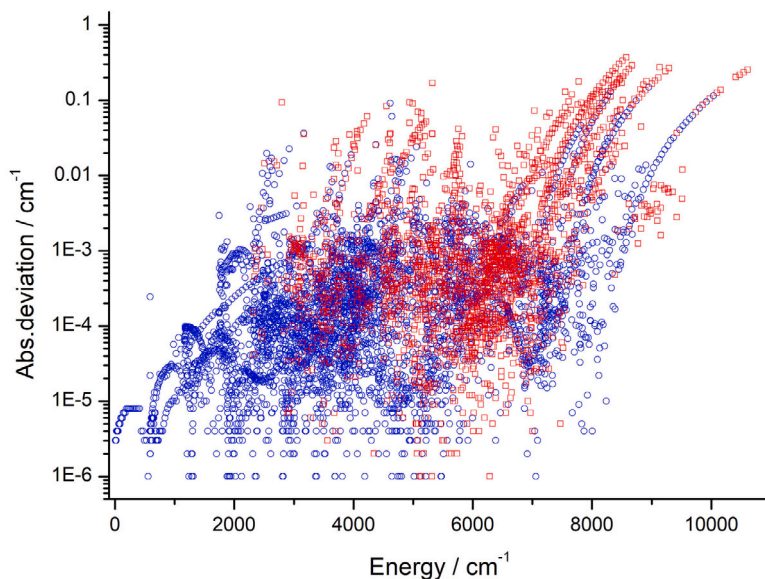


Fig. 3. Absolute deviations between the empirical (MARVEL) energy levels of this study and those of 04Toth [125]. Blue circles indicate states with MARVEL energies determined by at least three measured lines, while red squares correspond to the states with MARVEL energies determined by one or two measured lines.

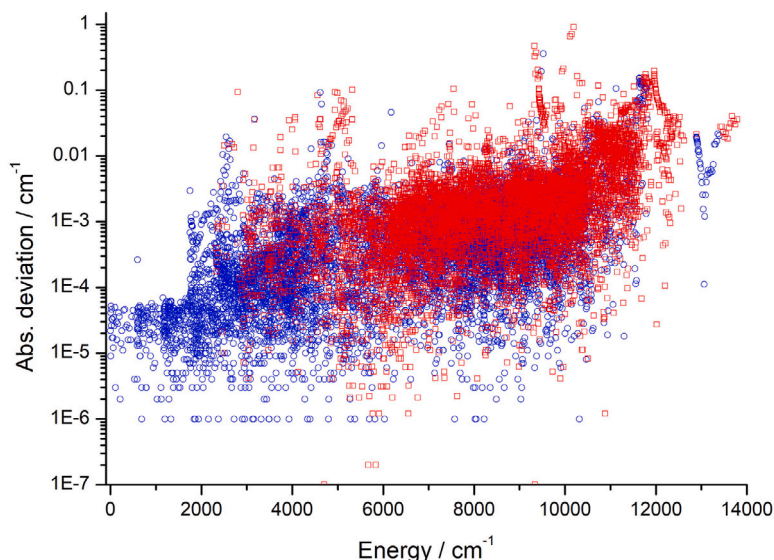


Fig. 4. Absolute deviations between the empirical (MARVEL) energy levels of this study and those of the NOSL-296 line list [179]; see text for the subset of NOSL-296 levels which could be utilized for this comparison. Blue circles indicate states with MARVEL energies determined by at least three measured lines, while the red squares correspond to the states with MARVEL energies determined by one or two measured lines.

blue circles in Fig. 4), in this case the average absolute difference is 0.0015 cm^{-1} ; (b) in the second step we compared those MARVEL levels with the NOSL-296 energies that are determined by one or two measured lines (see the red squares in Fig. 4). Although the average discrepancy is only 0.0054 cm^{-1} , in this case we get several outliers, where the differences are larger than 0.01 cm^{-1} . Furthermore, we found 47 MARVEL energy levels which could not be found in the NOSL-296 energy level list within 1.0 cm^{-1} , most of these energy levels have a large polyad number ($P > 20$); these states are all present in both the Ames and our own variational line lists.

Using the first set of MARVEL energy list, we checked the NOSL-296 lines and collected those lines where the difference in the line positions is larger than 0.005 cm^{-1} . We found only 392 NOSL-296 lines that the MARVEL energies cannot reproduce within this limit. This list can be found in the Supplementary Material. These lines should be checked by the authors of NOSL-296.

5. Summary and conclusions

The present study has provided a comprehensive analysis of all the measured and assigned rovibrational lines of the parent isotopologue of nitrous oxide, $^{14}\text{N}_2^{16}\text{O}$. There are 91 sources considered in our final compilation, containing experimental wavenumbers with uncertainties and assignments. The experimental line data were analyzed and their assignments adjusted to a uniform set of polyads (P) and associated counting numbers (N). This canonical set of vibrational state assignments is recommended for future studies on the spectroscopy of nitrous oxide. The full list is given in the Supporting Material.

The corrected, self-consistent list of 67 930 rovibrational transitions contains 43 246 unique entries. This dataset underwent a Measured Active Rotational–Vibrational Energy Levels (MARVEL) analysis, yielding 17 561 empirical energy levels. These energy levels were validated using variational nuclear-motion calculations [177,201], the full details

of which will be published elsewhere [201]. Uncertainties for the empirical rovibrational energy levels were determined using a newly implemented bootstrap approach. We believe this approach yields more realistic uncertainties and, at least in part, compensates for both under- and overestimates of the published uncertainties of the transitions observed.

This study investigated more than 200 vibrational bands and yielded empirical energy values for 77 vibrational band origins (those with $\ell = 0$, where ℓ is the vibrational angular momentum quantum number). Our newly determined energy levels are being used to improve the $^{14}\text{N}_2^{16}\text{O}$ line list currently under construction both by providing energies to which an improved potential energy surface can be fit to and, in due course, which can be used to replace computed energies in the final line list.

Comparison with entries of the line lists SISAM [125] and NOSL-296 [179] revealed good overall agreement but also pointed out several minor issues with the data. Resolution of these problems requires future careful experimental and modeling studies.

CRedit authorship contribution statement

Jonathan Tennyson: Writing – original draft, Funding acquisition, Formal analysis, Conceptualization. **Tibor Furtenbacher:** Writing – original draft, Methodology, Formal analysis. **Sergei N. Yurchenko:** Formal analysis. **Attila G. Császár:** Writing – review & editing, Methodology.

Declaration of competing interest

The authors declare no competing financial interests.

Data availability

The data are included in the supplementary materials.

Acknowledgments

JT thanks the Distinguished Guest Scientists Fellowship Program-2022 of the Hungarian Academy of Sciences for funding his stays in Hungary and Zsolt Mezei for hosting him. We thank Oleg Polyansky for helpful discussions, Alain Campargue for supplying the transition line lists for 96Campargue [97] and 01CaWeTaPe [114], and Xinchuan Huang for making the Ames line list available prior to publication. This work was supported by the European Research Council (ERC) under the European Union's Horizon 2020 research and innovation program through Advanced Grant number 883830. The work performed in Budapest received support from the HUN-REN Hungarian Research Network and the National Research, Development, and Innovation Office (NKFIH, grant no. K138233). This paper supports work within the COST (European Cooperation in Science and Technology) action CA21101 "Confined molecular systems: from a new generation of materials to the stars (COSY)".

Appendix A. Notes on data sources

Some sources, notably 60TiPIBe [17], 70PeSuFr [30], 74FaDu [44], and 18LaScAgMe [157], used the (c,d) notation instead of the (e,f) one [209]. We assumed that c corresponds to e and d to f. All other comments are listed source by source.

50HeHe [7]: This older source was the first detailed study of the near-infrared transitions in N_2O . By modern standards, it is relatively inaccurate, claiming a precision of 0.03 cm^{-1} for unblended lines. The source gives a calibration uncertainty of 0.08 cm^{-1} . However, there appears to be no subsequent high resolution measurements of the $(P\ell N) = (22\ 0\ 4)$ band centered at $11\ 964.3\text{ cm}^{-1}$. Recalibration of this source by a factor of 0.999 998 11 corresponds to a shift of -0.02 cm^{-1} .

Therefore, we adopted an uncertainty of 0.03 cm^{-1} , which was doubled for lines marked as blended with either other N_2O transitions or water lines.

60TiPIBe [17]: This source presents measurements of 2522 lines for a large number of vibrational bands. However, for most bands the values given are calculated with an unsigned obs–calc, meaning that it is not possible to reliably recover the experimental wavenumbers. Only 884 lines (for which there is no effective Hamiltonian fit given) were retained as these correspond to the actual measured wavenumbers: these lines are in any case for the more interesting (i.e., less studied) bands. The paper implies an uncertainty of 0.002 cm^{-1} but the lines retained are only given to two decimal digits; thus, these uncertainties were increased.

64LaLi [22]: No 'e'/'f' designation was given for transitions within the $02^2\ 0 [(P\ell N) = (22\ 1)]$ state; thus, these transitions were assumed to be degenerate and each line was included twice in our MARVEL database.

71LeHoThMa [33]: This source gives five transitions corresponding to $J = 3 - 2$ transitions in low-lying vibrational bands. As no uncertainties were given, 100 kHz was assumed by us. One of these measurements was not consistent with subsequent studies and had to be removed.

74FaDu [44]: Provides an unusual early fluorescence spectrum. The tables which were scanned are of poor quality, which gives some uncertainty over precise values for some of the lines.

74KrSa [46]: The authors did not specify uncertainties; thus, 0.02 cm^{-1} was assumed, with 0.04 cm^{-1} for blended lines, based on the use of combination differences. Transitions involving degenerate bands did not give 'e'/'f' parities; thus, they were included twice.

74BuVaGeKa [43]: The uncertainties attached to the transitions of this source were doubled, as suggested in 78Lovas [210].

75Bogey [49]: This source gives pure rotational transitions within the $(P\ell N) = (40\ 1)$ vibrational state. As suggested by 14TiChChCh [146], the uncertainties of this source should be increased as there are calibration issues with the data. The uncertainties were increased by a factor of three compared to the original values quoted in the paper.

75WhSuRiHa [54]: An uncertainty of 25 kHz was assumed.

76AmGu [55]: This publication is an early example of a high-accuracy infrared spectrum (with an uncertainty of $0.000\ 2\text{ cm}^{-1}$). The transitions are given as a comprehensive table in the paper but, unfortunately, with poor print quality. The results were extensively cleaned but even then there were many cases where the transition wavenumber could not be read with certainty. These cases were marked as not validated. The $(7\ 3\ 1) - (3\ 3\ 1)$ band was not given a parity, so it was assumed to represent both parities and duplicated. Transitions in the region where the $(6\ 0\ 2)$ and $(6\ 0\ 3)$ states interact were not consistent with those measured subsequently; therefore, they were removed from the analysis. Calibration tests suggested that the calibration of the spectrum was in line with more modern sources.

76AnBuKaKr [56]: This source contains a number of high-resolution pure rotational transitions. The fine structure (e/f) splitting within the $(3\ 3\ 1)$ state was not resolved, each line is given twice, and the uncertainties were increased to 35 kHz.

78ReMeDy [58]: This paper presents hyperfine-resolved rotational transitions. A simple average was performed over the hyperfine components and the uncertainty was set to 150 Hz.

82Guelachv [63]: The wavenumbers of this study were scaled by a calibration factor of 0.999 999 890, which is in line with later suggestions that the spectrum needs recalibration by about 15 MHz.

84Toth [67]: A wavenumber uncertainty of $0.000\ 2\text{ cm}^{-1}$ was chosen based on combination differences.

87HiWeMa [72]: The fine structure (e/f) splitting within the $(3\ 3\ 1)$ state was not resolved; thus, each line is given twice and the uncertainties were increased to 35 kHz.

95CaPeBaTe [93]: The wavenumbers were scaled by a calibration factor of 1.000 003 08.

96TaEvZiMa [100]: As suggested by 14TiChChCh [146], the uncertainties were increased by a factor of 1.6. The ν_1 and ν_3 vibrational state labels were swapped.

96MaRaHeVa [99]: The authors studied pressure shifts for two lines in the ν_3 or (2 0 2) band. However, the stated zero pressure line positions do not agree well with other measurements; thus, these lines were not validated.

96WeSiRe [101]: An uncertainty of 0.0006 cm^{-1} was assumed.

98GaCaKaSt [105]: The authors declare an uncertainty of 0.005 cm^{-1} ; this was doubled to 0.01 cm^{-1} for lines blended with water lines. It was necessary to reassign the P branch lines.

99Toth [110]: This paper reports a number of resonance interactions. Those involving the (8 0 3) and (8 0 4) bands do not give consistent combination differences and the associated transitions were removed. For other resonance pairs the uncertainties were increased.

00WeKaCaBa [111]: This source reports both ICLAS and FTS transition wavenumbers. For the ICLAS data an uncertainty of 0.005 cm^{-1} is given; lines marked as blended or weak were given an uncertainty of 0.01 cm^{-1} . For the FTS data, 0.0005 cm^{-1} was used below 6300 cm^{-1} , which was linearly increased to 0.0055 cm^{-1} at 11300 cm^{-1} as suggested in the paper. The J 's in the (18 0 3) – (0 0 1) band's R branch transitions were renumbered. Resonance lines in the (13 1 7) – (1 1 1) hot band were assigned to (13 1 6) – (1 1 1). The P(12) line in the (20 0 2) – (0 0 1) band (line 00WeKaCaBa.12) was changed from 10818.2090 to 10808.2090. Extra resonance lines P(32) (06WaPeTaGa.2327) and P(33) (06WaPeTaGa.2328) in the band (16 0 7) – (0 0 1) were assigned to (16 0 6) – (0 0 1).

01BaVe [113]: Bands for which the e/f splitting was unresolved were duplicated. An uncertainty of 0.008 cm^{-1} (given as the upper limit in the paper) was adopted.

01CaWeTaPe [114]: An uncertainty of 0.015 cm^{-1} was assumed, except for lines designated as lines overlapping with atmospheric water lines, lines overlapping with other N_2O lines, or very weak lines, for which an uncertainty of 0.030 cm^{-1} was adopted.

03BaPiVe [118]: This source gives three bands with unresolved e/f splitting, each were included in our analysis twice. Uncertainty estimated as 0.0004 cm^{-1} , based on data in the paper.

03DiPeTaTe [119]: An uncertainty of 0.003 cm^{-1} was adopted from the paper, except for blended or degenerate lines, for which an uncertainty of 0.006 cm^{-1} was used. For band (16 0 17) – (0 0 1), the lines R(32) – R(36) were removed, as they have been reassigned by 04BeCaPeTa.

04BeCaPeTa [123]: An uncertainty of 0.005 cm^{-1} was taken from the paper; for lines marked as blended with water lines this uncertainty was doubled. The paper includes correction of a few misprints in the rovibrational parameters and the reconsideration of the analysis of an inter-polyad Coriolis interaction system given in 03DiPeTaTe [119]. Resonance lines in (16 0 17) – (0 0 1) were re-assigned to the e branch of (17 1 6) – (0 0 1). Three lines overlapping with water lines were removed as they were inconsistent with other sources.

04NeSuVa [124]: An uncertainty of 0.0005 cm^{-1} was adopted from the paper.

04Toth [125]: This source is discussed in Section 4.1.

06HePiGuSo [128]: Q branches (both e – f and f – e) in the (9 1 9) – (3 1 1) band were removed as they are inconsistent with other transitions given in this source and elsewhere, such as 19BeMoKaKa [158]. Eleven lines were removed as they involve J values lower than the ℓ value of the given vibrational state, which is unphysical. The six highest P(J) lines from the (10 2 4)e – (3 1 1)e band were removed as they disagree with other sources, notably 19BeMoKaKa [158], where the assignments are confirmed by combination differences. The (2 2 1)f band was removed as it was assigned using an incorrect value for the D centrifugal distortion constant, taken from Toth [125], and therefore gave wavenumbers which disagree with other sources. This source also includes corrections of a few misprints in the rovibrational

parameters and the reconsideration of the analysis of an interpolyad Coriolis interaction system given in 03DiPeTaTe [119].

06WaPeTaGa [129]: An uncertainty of 0.005 cm^{-1} was adopted from the paper, except for lines blended with water lines, for which an uncertainty of 0.01 cm^{-1} was assumed. The band (14 0 8) – (0 0 1) centered at 7998.59 cm^{-1} has extra lines for $J = 28$ and 29 , presumably due to resonances. The interacting state is unassigned so the extra lines were removed. The R(28) and R(29) lines in the (11,1,11) f – (1,1,1) f band were reassigned to R(29) and R(30), respectively. This source contains 908 lines which are exactly the same as in 00WeKaCaBa [111]. Since lists of co-authors of these two publications contain no overlaps, both sets of lines were kept.

07Horneman [132]: Following 14TiChChCh [146], all transitions in the (1 1 1) – (0 0 1) band were retained, even those with zero weights in the fit. Nevertheless, 24 lines had to be removed, on the basis of inconsistency with other sources, including transitions in the (2 0 0) – (1 1 1) and (2 2 1) – (1 1 1) bands, which were zero-weighted in the original paper. 14TiChChCh [146] states it is necessary to remove 38 lines from 07Horneman but does not specify which.

07LiKaMaRo [133]: Q branches for bands with $\ell > 0$ for both upper and lower states have the wrong selection rules (e – e or f – f). We assumed that the parity of the lower state is given correctly on the basis of consistency with other sources. On this basis the following corrections were made (in the harmonic oscillator notation used in the original source): $52^2\text{Of} - 02^2\text{Of}$ to $52^2\text{Oe} - 02^2\text{Of}$; $35^1\text{Oe} - 01^1\text{Oe}$ to $35^1\text{Of} - 01^1\text{Oe}$; $35^1\text{Of} - 01^1\text{Of}$ to $35^1\text{Oe} - 01^1\text{Of}$; $02^2\text{3e} - 02^2\text{Oe}$ to $02^2\text{3f} - 02^2\text{Oe}$; $02^2\text{3f} - 02^2\text{Of}$ to $02^2\text{3e} - 02^2\text{Of}$; $51^1\text{Oe} - 01^1\text{Oe}$ to $51^1\text{Of} - 01^1\text{Oe}$; $51^1\text{Of} - 01^1\text{Of}$ to $51^1\text{Oe} - 01^1\text{Of}$. The $36^2\text{O} - 02^2\text{O}$ band does not have the ℓ -doubling resolved; thus, it was given twice with the correct selection rules. Lines P(19)–P(36) in the $32^0\text{1e} - 02^0\text{0e}$ band were reassigned to P(18)–P(35); lines P(16)–P(18) in the $36^2\text{0e} - 02^2\text{0e}$ band were reassigned to P(15)–P(17). Line Q(22) in the $35^0\text{1f} - 01^1\text{0f}$ band was reassigned to Q(23). Lines Q(16)–Q(18) in the $51^1\text{0e} - 01^1\text{0f}$ band were reassigned to Q(17)–Q(19). Finally, the Q(10) line at $6302.6551 \text{ cm}^{-1}$ in the (1 1 1 1)e – (1 1 1)f band was reassigned to the (1 2 2 1)e – (1 1 1)f band. This source contains 90 lines which appear to be duplicates of lines in 99Toth [110]. These duplicate lines were kept during the MARVEL analysis. Furthermore, this source contains 47 lines which also appear in 09LiKaPeHu [136]. These duplicate lines were kept only here.

07LiKaPeTa [134]: The band centered at about 6770 cm^{-1} given as $0^*10\text{e} - 0000\text{e}$ is assumed to be $0(11)0\text{e} - 0000\text{e}$, which is (1 1 1 10)e – (0 0 1)e in polyad notation. In the R branch of the (10 0 9)e – (0 0 1)e band lines R(51)–R(55) were reassigned to R(50)–R(54). This source contains 172 lines which also appear in the source 09LiKaPeHu [136]. The identical lines were only kept here.

09LiKaPeHu [136]: Both the e and f components of the (14 2 15) – (2 2 1) band contained an unresolved P(2) line at $6836.0365 \text{ cm}^{-1}$, which are unphysical and thus were removed. Line R(58) in the (13 1 7)e – (1 1 1)e band was reassigned to R(57). Line R(42) in the (14 2 5)e – (2 2 1)e band was reassigned as R(42)f. This source contains 55 lines which also appear in the source 12LuMoLiPe [142]. These identical lines were only kept here.

11LiKaPeTa [140]: This source contains 391 lines which also appear in the source 12LuMoLiPe [142]. These lines were deleted in the list of lines of 12LuMoLiPe.

12LuMoLiPe [142]: Line 12LuMoLiPe.3047, assigned as P(1) (13 1 4) e – (0 0 1)e, was removed as being unphysical.

16KaCaKaPe [150]: The R(39) line at $7989.89025 \text{ cm}^{-1}$, assigned as $35^1\text{1f} - 01^1\text{0f}$ in the original paper, was reassigned to $31^1\text{1f} - 01^1\text{0f}$ or (15 1 8)f, in line with its neighboring transitions. Four lines reassigned and given by 22KaTaKaCab [175] were removed. 526 lines recorded by 16KaCaKaPe but assigned by 22KaTaKaCab were added. Lines 16KaCaKaPe.3134 and 16KaCaKaPe.3135 denoted as “extra lines” by 22KaTaKaCab were assigned to the band (15 1 7)e – (1 1 1)e. This source contains 171 duplicate transitions, we kept one of the duplicate entries.

19BeMoKaKa [158]: Assignments of the (1005)e and (1006)e bands were swapped.

20ZhBaFIHo [164]: The stated frequencies were doubled to allow for two-photon transitions; the corresponding uncertainties were also doubled.

21KaKaTaCa [170]: No uncertainty is stated; a value of 0.001 cm^{-1} was assumed.

22KaTaKaCaa [174] Nine lines in the range 22KaTaKaCaa.2461 to 22KaTaKaCa.2505 were reassigned to (16019)e instead of (16017). The P(36) line at $8556.24190\text{ cm}^{-1}$ was reassigned from (1804)e – (202)e to (1711)e – (202)e. This source contains two duplicated transitions, we deleted one of the duplicated entries.

22KaTaKaCab [175]: Ten lines identified as in resonance with (1518) assigned to (1517); six lines identified as in resonance with (16010) assigned to (16216). 526 lines measured by 16KaCaKaPe [150] were assigned; these are the last lines labeled as 16KaCaKaPe. Resonances lines in the (1627) – (221) band involving $J' = 35$ and 36 were reassigned to (15113) – (221), as suggested in the paper. This source contains 28 duplicated transitions, we had to delete one duplicate entry.

22LuGo [176]: An uncertainty of 0.01 cm^{-1} was assumed, except for lines marked as blended, for which 0.02 cm^{-1} was used.

24SiSeEmMa [180]: After the original submission of our paper, this new source became available and was added as part of the revision process. Bands (1804), (1808) and (1809) were relabeled (1803), (1807) and (1808), respectively, in line with our proposed canonical numbering scheme. Four lines which do not obey combination differences, even within the 24SiSeEmMa dataset, were removed.

Appendix B. Supplementary material

See supplementary material for the MARVEL input (transitions) file and output (energy) file. A comprehensive table of vibrational levels with associated polyad quantum number is also given.

Supplementary material associated with this article can be found, in the online version, at <https://doi.org/10.1016/j.jqsrt.2024.108902>.

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