# High sensitivity ICLAS of $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ in the region of the second decade ( $11520-12810 \mathrm{~cm}^{-1}$ ) 

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#### Abstract

The high resolution absorption spectrum of the $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ isotopologue of water has been recorded by Intracavity Laser Absorption Spectroscopy (ICLAS) with a sensitivity on the order of $\alpha_{\min } \sim 10^{-9} \mathrm{~cm}^{-1}$. The $11520-12810 \mathrm{~cm}^{-1}$ spectral region corresponding to the $3 v+\delta$ decade of vibrational states, was explored with an ICLAS spectrometer based on a Ti:Sapphire laser. It allowed detecting transitions with an intensity down to $10^{-27} \mathrm{~cm} /$ molecule which is about 100 times lower than the weaker line intensities available in the literature, in particular in the HITRAN database.

The rovibrational assignment was performed on the basis of the results of variational calculations and allowed for assigning 3659 lines to the $\mathrm{H}_{2}{ }^{16} \mathrm{O}, \mathrm{H}_{2}{ }^{18} \mathrm{O}, \mathrm{H}_{2}{ }^{17} \mathrm{O}, \mathrm{HD}^{16} \mathrm{O}$ and $\mathrm{HD}^{18} \mathrm{O}$ species, leaving only $1.7 \%$ unassigned transitions. A line list including 1712 transitions of $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ has been generated and assigned leading to the determination of 692 rovibrational energy levels belonging to a total of 16 vibrational states, 386 being newly observed. A deviation on the order of $25 \%$ has been evidenced for the average intensity values given by HITRAN and the results of variational calculations. Ninety two transitions of the $\mathrm{HD}^{18} \mathrm{O}$ isotopologue could also be assigned and the corresponding upper rovibrational levels are given.


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## 1. Introduction

With about $0.2 \%$ abundance, $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ is the most abundant isotopologue of water after $\mathrm{H}_{2}{ }^{16} \mathrm{O}$. It is considered as the fifth atmospheric absorber. This is why the precise characterization of its absorption spectrum is of significant importance for atmospheric modeling, in particular in the near infrared and visible spectral regions. Most of the experimental information concerning water has been obtained by Fourier Transform Spectroscopy (FTS) which has the advantage of allowing for a wide spectral coverage and a good sensitivity when associated with long multi-pass cells. In particular, the spectroscopic parameters obtained from FTS spectra are generally those adopted in the HITRAN database [1].

[^0]In the present contribution, the weak absorption spectrum of an ${ }^{18} \mathrm{O}$ enriched sample of water has been recorded by Intracavity Laser Absorption Spectroscopy (ICLAS) in the $11520-12810 \mathrm{~cm}^{-1}$ spectral region which covers the $3 v+\delta$ decade. The overview of the investigated region, as provided by different databases, is presented in Fig. 1. To our knowledge, the only absorption spectra of the $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ isotopologue available near $12500 \mathrm{~cm}^{-1}$ were obtained in the 1980s, by Chevillard et al. [2-4] at Kitt Peak National Solar Observatory. The FTS spectrometer was associated with a 6 m long White cell allowing absorption path lengths up to 434 m and the spectral resolution was $0.012 \mathrm{~cm}^{-1}$. The analysis of these spectra in our region of interest has been reported in the following contributions:
(i) Bykov et al. [5] analyzed the $11300-12710 \mathrm{~cm}^{-1}$ region using the effective Hamiltonian approach


Fig. 1. Comparison of the $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ spectrum between 11500 and $12800 \mathrm{~cm}^{-1}$ : (a) HITRAN database [1], (b) FTS spectrum recorded at Kitt Peak [5], (c) Results of Schwenke and Partridge calculations [19,20], (d) ICLAS (this work). The dashed region corresponds to relatively strong line intensities which are saturated on the ICLAS spectra and cannot be used for line intensity retrieval. The intensity cut off was fixed to a value of $5 \times 10^{-25} \mathrm{~cm} /$ molecule. All the intensities correspond to pure $\mathrm{H}_{2}{ }^{18} \mathrm{O}$.
and could determine 315 energy levels from the observation of 765 transitions reaching the (131), (211), (013), (230), (310) and (112) vibrational states
(ii) More recently, Tanaka et al. $[6,7]$ reanalyzed these spectra in the $12400-14520 \mathrm{~cm}^{-1}$ region and could assign additional transitions by using recent results of variational calculations. Note that the line list attached to Ref. [7] is the one adopted in the 2004 version of the HITRAN database [1].

Laser-based techniques successfully compete with FTS associated with long multipass cells, in detecting weak transitions. In the case of less abundant isotopologues, techniques such as ICLAS or Cavity Ring Down Spectroscopy (CRDS), have the additional advantage of requiring a very small quantity of gas (typically $10^{-3}$ mol). For instance, the spectrum of $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ in the region of the $5 v$ polyad has been recorded by pulsed CRDS spectrometer with sensitivity on the order of $2 \times 10^{-26} \mathrm{~cm} /$ molecule [8]. The $11000-14000 \mathrm{~cm}^{-1}$ region is easily accessible by using a Ti : Sapphire laser and ICLAS investigations of a large variety of molecules have been reported in this range [9]. For instance, ICLAS-Ti:Sa was applied to the study of deuterated water with a detection scheme based either on a grating spectrograph [10] or a FTS spectrometer [11,12]. We have recently reported [13] the detection of weak lines of the water main isotopologue near $12000 \mathrm{~cm}^{-1}$ with a sensitivity as low as $10^{-27} \mathrm{~cm} /$ molecule i.e. at least one order of magnitude beyond the performances of the best FTS experiments [1,14-16]. In the case of $\mathrm{H}_{2}{ }^{18} \mathrm{O}$, a two orders of magnitude gain in sensitivity is expected as the weakest lines detected in the Kitt Peak spectra have intensity on the order of $10^{-25} \mathrm{~cm} /$ molecule (see Fig. 1).

## 2. Experiment and line list construction

Our ICLAS spectrometer has been previously described in Refs. $[9,17,18]$ and very recently in our work devoted to $\mathrm{H}_{2}{ }^{16} \mathrm{O}$ in the same spectral region [13]. The spectra were recorded with a generation time ranging between 50 and $150 \mu \mathrm{~s}$ corresponding to an equivalent absorption path length of 4.8 and 14.4 km , respectively, as the filling ratio of the laser cavity by the absorption cell is $32 \%$. In order to minimize the contribution of the intracavity atmospheric absorption (mainly due to $\mathrm{H}_{2}{ }^{16} \mathrm{O}$ ), the laser was placed in a box filled with dry nitrogen. The experimental procedure consisted in successively filling the cell with water, recording the spectrum, vacuuming the cell and recording the background spectrum. Typically, a few seconds of averaging were necessary to record a spectral window, owing to the frequency multiplex advantage of ICLAS when used with a dispersion spectrometer. The algebraic division of the spectrum by the background spectrum is a very efficient method to suppress stable spectral features frequently present in the ICLAS spectra and to increase of the signal to noise ratio. In particular, fringes due to FabryPerot type interferences between the fixed optical elements in the laser cavity, are totally removed by this procedure.

The grating spectrograph ( 79 grooves $/ \mathrm{mm}$ ) works in a high order of diffraction (about 30) allowing for a practical spectral resolution close to the doppler line width ( $0.015 \mathrm{~cm}^{-1}$ (HWHM) at $12000 \mathrm{~cm}^{-1}$ ). The region simultaneously recorded with our 3754 diodes silicon array is about $14 \mathrm{~cm}^{-1}$ wide according to the dispersion of the grating spectrograph. The wavenumber calibration of each individual spectrum requires the correction of the non linear dispersion of the grating spectrograph by using the equidistant frequency comb provided by an intracavity étalon and the use of reference lines to calibrate accurately the wavenumber scale. As we will see below, the proportion of $\mathrm{H}_{2}{ }^{16} \mathrm{O}$ and $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ molecules in our sample was about 45 and $55 \%$, respectively so that the observed spectrum exhibits many transitions of the main water isotopologue which were adopted as reference lines. The corresponding $\mathrm{H}_{2}{ }^{16} \mathrm{O}$ line positions were taken in the most complete set available in the literature. It resulted in using the line lists attached to Ref. [16] and Ref. [15] for the $11520-12350 \mathrm{~cm}^{-1}$ and $12350-$ $12780 \mathrm{~cm}^{-1}$ spectral regions, respectively. The estimated experimental accuracy concerning the wavenumber calibration was about $0.003 \mathrm{~cm}^{-1}$, which is smaller than the frequency binning of the recording CCD array.

The $1300 \mathrm{~cm}^{-1}$ wide spectral section presently investigated was covered by a total of 140 spectral snapshots. The window overlap was about $4 \mathrm{~cm}^{-1}$ on each side. A series of measurements with pressures ranging between 1 and 20 Torr was recorded in order to measure weaker lines at high pressure and well resolved stronger lines at low pressure.

## Relative intensity of the $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ transitions

For each $14 \mathrm{~cm}^{-1}$ wide spectral window, a related file was created containing a list of the line centers and the corresponding transition relative intensities. Considering the number of lines which were frequently overlapped (it was found that about $5 \%$ of the lines strongly overlapped in our final line list.), the line intensity determination was difficult and time consuming. The typical pressure broadening ( $0.0025 \mathrm{~cm}^{-1}$ (HWHM) at 20 Torr) is much smaller than the Doppler broadening ( $0.017 \mathrm{~cm}^{-1}$ (HWHM)). A gaussian function was then adopted as approximate line profile. Isolated lines were fitted by the help of a homemade software which saved the line centre as well as the integrated absorbance obtained from the fit. In the case of strong and less strong overlapping lines, the integrated absorbance (or line strength) was estimated from the absorbance value at the line centre and the average line width value of the well isolated nearby lines. Finally in case of weak overlapping lines, a multi-gaussian fit was performed.

## Absolute intensity of the $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ transitions

ICLAS is a quantitative method which provides accurate absolute intensity values [9]. However, as a result of a relatively large uncertainty on our pressure values, we decided to obtain absolute intensity values simply by scaling the relative line strengths obtained as described above, to the line strength values provided by the HITRAN database. As the HITRAN database provides $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ lines only in the $12400-12800 \mathrm{~cm}^{-1}$ region (see Fig. 1), we could calibrate only a small part of the spectral windows against $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ reference lines. We hence used the $\mathrm{H}_{2}{ }^{16} \mathrm{O}$ lines (from Refs. [ 15,16$]$ ) in the $12400-12800 \mathrm{~cm}^{-1}$ region to determine the isotopic abundance ratio between the two isotopologues. The ICLAS relative intensities were then scaled versus the $\mathrm{H}_{2}{ }^{16} \mathrm{O}$ absolute line intensities at 296 K over the whole studied spectral region and converted into absolute intensities for pure $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ by using the determined concentration ratio. A value of $0.55(7) / 0.45(6)$ was obtained for the $\mathrm{H}_{2}{ }^{18} \mathrm{O} / \mathrm{H}_{2}{ }^{16} \mathrm{O}$ by averaging the values obtained from spectral windows allowing for an independent calibration of the $\mathrm{H}_{2}{ }^{16} \mathrm{O}$ and $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ line transitions. The uncertainties in the isotopic ratio are equal to the standard deviation of the ratios obtained on different spectral windows. It was found that because of water adsorption on the sample cell walls, the isotopic ratio slightly changed from spectrum to spectrum. Note that as the stronger lines were frequently saturated in the ICLAS spectrum and as they have been previously accurately measured by FTS, we decided to pay mainly attention to the lines with intensity lower than $5 \times 10^{-25} \mathrm{~cm} /$ molecule. This maximum value is a factor of 10 larger than the typical sensitivity of the Kitt Peak spectrum (see Fig. 1). It is difficult to estimate the uncertainty of our line intensities as it depends on the accuracy of the $\mathrm{H}_{2}{ }^{16} \mathrm{O}$ line intensities used as references, of the determined isotopic ratio and of our relative intensities values which
are probably not fully satisfactory in the case of weak and blended lines. We cannot rule out error on the order of $100 \%$ for the intensities of the weakest lines, while in the ideal cases of well isolated lines of medium intensity, a few $\%$ accuracy is probably achieved.

## Global line list

The most complete list of 9615 lines (including all water isotopologues) was created simply by gathering all the lines measured on the 140 individual spectral windows. Many lines appear several times in this list as a consequence of the existence of overlapping regions and of several recordings of the same spectral windows at different pressures. We decided to consider as identical two lines for which the two following criterions were satisfied (i) wavenumber difference less than $8 \times 10^{-3} \mathrm{~cm}^{-1}$ and (ii) line strength differed by at most a factor of 2 for weak lines just above the noise level. By averaging the position and intensities of these identical lines (including all water isotopologues), the number of lines was decreased from 9615 to 3624 which is the line list considered in the forthcoming rovibrational analysis. The line list including rovibrational assignments, Schwenke and Partridge (SP) calculated positions and intensities [19,20], is attached to the paper as Supplementary Material. For convenience of the user, we have completed this line list with 177 stronger $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ lines previously measured by FTS as they could not be accurately measured by ICLAS because of saturation effects. The line positions of these strong lines were taken from Ref. [5] and the corresponding SP line intensities are given.

## 3. Line assignment and energy level derivation

Five water isotopologues were found to contribute to the observed spectrum: $\mathrm{H}_{2}{ }^{16} \mathrm{O}, \mathrm{H}_{2}{ }^{18} \mathrm{O}, \mathrm{H}_{2}{ }^{17} \mathrm{O}, \mathrm{HD}^{16} \mathrm{O}$, and $\mathrm{HD}^{18} \mathrm{O}$. For each of these species, the assignment was based on the results of SP calculations [19,20] as available on the web-based spectroscopic information system SPECTRA of the Institute of Atmospheric Optics in Tomsk, Russia (http://spectra.iao.ru). The calculated intensities were scaled to match on average the corresponding experimental values. The correspondence between the experimental and calculated lines was found by using the usual criteria: agreement in frequencies and intensities, combination difference relations and smooth dependence versus the rotational quantum numbers, of the difference between the experimental energy level and SP calculated values. In a second step, the assignments to each isotopologue were checked against their known experimental levels and corrected when necessary; the major attention being given to $\mathrm{H}_{2}{ }^{18} \mathrm{O}$. The previous experimental studies relevant for this checking are the followings: $\mathrm{H}_{2}{ }^{16} \mathrm{O}[13,15$ and 16], $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ [5-7], $\mathrm{H}_{2}{ }^{17} \mathrm{O}$ [7] and $\mathrm{HD}^{16} \mathrm{O}$ [10]. As a result, the number of lines assigned for each isotopologue is: $\mathrm{H}_{2}{ }^{16} \mathrm{O}$ : 1553, $\mathrm{H}_{2}{ }^{18} \mathrm{O}: 1712, \mathrm{H}_{2}{ }^{17} \mathrm{O}: 326, \mathrm{HD}^{16} \mathrm{O}: 68$ and $\mathrm{HD}^{18} \mathrm{O}$ :

92 , leaving unassigned only 61 lines ( $1.7 \%$ ). Two examples of spectra assignment are given in Figs. 2 and 3.

The new experimental information derived from this analysis concerns the $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ and $\mathrm{HD}^{18} \mathrm{O}$ isotopologues and we will then limit the further discussion to these species. In the investigated spectral region, no transition was previously reported for the $\mathrm{HD}^{18} \mathrm{O}$ isotopologue. As illustrated in Figs. 1-3, the two orders of magnitude gain in sensitivity achieved by ICLAS compared to Kitt Peak spectra allows extending importantly the knowledge of the $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ species: over the 1712 transitions assigned to $\mathrm{H}_{2}{ }^{18} \mathrm{O}, 774$ were found to reach new energy levels. It resulted in the derivation of 692 energy levels belonging to 16 vibrational states, 386 of them being newly determined. The upper level energies were derived by adding the lower energy values [21] to the observed transitions. About $47 \%$ and $18 \%$ of the predicted transitions with line strengths in the range $2 \times 10^{-27}-5 \times 10^{-25}$ and $1 \times 10^{-26}$ $5 \times 10^{-25} \mathrm{~cm} /$ molecule, respectively, were not observed. These percentages give an evaluation of the fraction of weak $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ lines obscured by strong lines of $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ or $\mathrm{H}_{2}{ }^{16} \mathrm{O}$.

A state by state comparison with previous FTS analysis is presented in Table 1. The corresponding total number of levels determined by Bykov et al. [5] in the $11300-$ $12710 \mathrm{~cm}^{-1}$ region and Tanaka et al. [7] in the wider $12400-14520 \mathrm{~cm}^{-1}$ region, were 315 and 365 , respectively. The whole set of energy levels is listed in Tables 2-4 in which the deviations of the observed levels from their calculated values [19] are also included. These tables give the uncertainty on the energy level value when determined through different transitions. Additional information about the quality of the energy levels can be found in the energy


Fig. 2. $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ spectrum in a spectral section around $11605 \mathrm{~cm}^{-1}$ : (a) ICLAS spectrum recorded with an ${ }^{18} \mathrm{O}$ enriched sample of water (total pressure: 18 hPa , absorption equivalent pathlength of 14.4 km corresponding to a $150 \mu$ s generation time). (b) Stick spectrum of the $\mathrm{H}_{2}{ }^{16} \mathrm{O}$ (dashed line) and $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ (solid lines) retrieved from the ICLAS spectrum. The line intensities correspond to pure $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ and the $\mathrm{H}_{2}{ }^{16} \mathrm{O}$ line intensities were scaled to best match the above ICLAS spectrum, (c) Results of Schwenke and Partridge variational calculations for $\mathrm{H}_{2}{ }^{18} \mathrm{O}[19,20]$. Note that only the two strongest lines of the region were detected in Kitt Peak FTS [5].


Fig. 3. Comparison of $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ spectrum in a spectral section around $12035 \mathrm{~cm}^{-1}$ : (a) ICLAS spectrum recorded with an ${ }^{18} \mathrm{O}$ enriched sample of water (total pressure 18 hPa , absorption equivalent path length of 4.8 km corresponding to a $50 \mu$ s generation time) showing the contribution of different isotopologues. The $\mathrm{H}_{2}{ }^{16} \mathrm{O}$ and $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ species are easily identified by comparison with (b) while the $\mathrm{H}_{2}{ }^{17} \mathrm{O}, \mathrm{HD}^{16} \mathrm{O}$, and $\mathrm{HD}^{18} \mathrm{O}$ isotopologues are marked by 171,162 and 182, respectively, (b) Stick spectrum of the $\mathrm{H}_{2}{ }^{16} \mathrm{O}$ and $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ isotopologues retrieved from the ICLAS spectrum. The line intensities correspond to pure $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ and the $\mathrm{H}_{2}{ }^{16} \mathrm{O}$ line intensities were scaled to match approximately the above ICLAS spectrum, (c) Results of the Schwenke and Partridge [19,20] variational calculations for $\mathrm{H}_{2}{ }^{18} \mathrm{O}$, (d) Kitt Peak stick $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ spectrum [5].
level file provided in the Supplementary Material. For each rovibrational level, three labels are given to indicate if any problematic lines were used to derive the corresponding

Table 1
Comparison of the number of energy levels determined from the vibrational bands of $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ recorded by ICLAS between 11520 and $12810 \mathrm{~cm}^{-1}$ and the previous analysis of Kitt Peak FTS spectra [5,7]

| Vibrational <br> level | Vib. Term. <br> $\left(\mathrm{cm}^{-1}\right)$ | Number of observed levels <br> Ref. [7] | Ref. [5] |
| :--- | :--- | :---: | :---: |
| 003 | 10993.680 |  |  |
| ICLAS |  |  |  |

[^1]Table 2
Energy levels of the (230), (131), (032) and (310) vibrational states of $\mathrm{H}_{2}{ }^{18} \mathrm{O}$

| $J K_{a} K_{c}$ | (230) |  |  |  | (131) |  |  |  | (032) |  |  |  | (310) |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $E_{\text {obs }}\left(\mathrm{cm}^{-1}\right)$ | $\sigma$ | $N$ | $\Delta$ | $E_{\text {obs }}\left(\mathrm{cm}^{-1}\right)$ | $\sigma$ | $N$ | $\Delta$ | $E_{\text {obs }}\left(\mathrm{cm}^{-1}\right)$ | $\sigma$ | $N$ | 4 | $E_{\text {obs }}\left(\mathrm{cm}^{-1}\right)$ | $\sigma$ | $N$ | $\Delta$ |
| 000 | 11734.5250 |  | 1 | -100 | 11774.7067 |  | 1 | 33 | 11963.5372 |  | 1 | -77 | 12106.9776 |  | 1 | -28 |
| 101 | 11757.5444 |  | 1 | -95 | 11797.9134 | 0.7 | 2 | 40 | 11986.9193 |  | 1 | -77 | 12129.7423 |  | 1 | -18 |
| 111 | 11781.1470 | 2.1 | 2 | -92 | 11820.0649 |  | 1 | 42 | 12008.0046 |  | 1 | -78 | 12143.4722 | 1.6 | 3 | -25 |
| 110 | 11787.2915 | 0.6 | 2 | -91 | 11826.2574 | 1.9 | 2 | 24 | 12014.2761 | 2.5 | 2 | -80 | 12148.8514 | 1.1 | 2 | -21 |
| 202 | 11802.4850 | 0.2 | 2 | -95 | 11843.1421 | 2.2 | 2 | 42 | 12032.4360 |  | 1 | -77 | 12173.8481 |  | 1 | -26 |
| 212 | 11821.0773 | 1.2 | 3 | -88 | 11860.2638 | 0.5 | 3 | 42 | 12048.5290 | 2.2 | 3 | -74 | 12182.3718 | 0.6 | 2 | -26 |
| 211 | 11839.4607 | 1.4 | 3 | -87 | 11878.7945 | 0.3 | 3 | 21 | 12067.3082 |  | 1 | -78 | 12199.8482 | 2.0 | 2 | -17 |
| 221 | 11907.6526 | 0.5 | 4 | -82 | 11943.4263 | 0.7 | 2 | 40 | 12128.8570 | 0.7 | 2 | -64 | 12240.3412 | 1.7 | 2 | -28 |
| 220 | 11908.6823 |  | 1 | -74 | 11944.5510 |  | 2 | 40 |  |  |  |  | 12241.6729 |  | 1 | -19 |
| 303 | 11867.4124 | 0.8 | 2 | -91 | 11908.3252 | 7.4 | 2 | 18 | 12097.9170 | 0.0 | 2 | -74 | 12237.0421 | 4.0 | 3 | -11 |
| 313 | 11880.3344 | 0.5 | 3 | -92 | 11919.8856 | 0.3 | 2 | 44 |  |  |  |  | 12242.1141 | 1.5 | 3 | -30 |
| 312 | 11916.8492* | 0.1 | 2 | -85 | 11956.6456 | 1.2 | 3 | 42 | 12145.8749 | 0.9 | 2 | -71 | 12275.2578 | 3.1 | 2 | -5 |
| 322 | 11976.9670 | 0.2 | 2 | -64 | 12013.1143 | 0.9 | 2 | 46 | 12199.1587 | 0.6 | 2 | -74 | 12308.7365 | 1.2 | 3 | -13 |
| 321 | 11981.8795 | 0.6 | 4 | -69 | 12018.4578 | 1.9 | 2 | 24 | 12204.8414 | 1.9 | 3 | -76 | 12314.9049 | 1.3 | 4 | -9 |
| 331 | 12100.3934 |  | 1 | -62 | 12131.6774 | 1.3 | 3 | 35 | 12313.2082 |  | 1 | -68 | 12389.3307 |  | 1 | -9 |
| 330 | 12100.5457 | 0.9 | 3 | -56 | 12131.8089 | 0.3 | 2 | 35 | 12313.3584 |  | 1 | -83 | 12389.5364 | 0.1 | 2 | -7 |
| 404 | 11950.2671* |  | 1 | -82 | 11991.3860 |  | 1 | 55 | 12181.2242 | 0.5 | 2 | -70 | 12317.4386 | 0.9 | 2 | -12 |
| 414 | 11958.3165* | 0.8 | 3 | -73 | 11998.3053 | 0.9 | 3 | 50 | 12187.2535 | 3.4 | 2 | -76 | 12319.8877 | 0.6 | 3 | -13 |
| 413 | 12018.3083 | 0.1 | 2 | -87 | 12058.4330 | 1.2 | 4 | 40 | 12248.6140 |  | 1 | -63 | 12373.5062 | 2.0 | 3 | -13 |
| 423 | 12068.5898* | 0.7 | 3 | -50 | 12105.0025 | 2.9 | 3 | 20 | 12291.7524 | 1.3 | 3 | -71 | 12398.8016 | 1.3 | 5 | -5 |
| 422 | 12081.9985 | 2.4 | 2 | -63 | 12119.6118 | 1.1 | 3 | 52 | 12307.1822 |  | 1 | -62 | 12414.9323 | 1.0 | 4 | 1 |
| 432 | 12195.0479 | 0.5 | 4 | -43 | 12226.6838 | 1.6 | 4 | 42 | 12409.2437 | 2.4 | 3 | -80 | 12482.7504 | 2.0 | 2 | 2 |
| 431 | 12195.6045 |  | 1 | -57 | 12227.5749 | 0.2 | 3 | 41 | 12410.2696 |  | 1 | -64 | 12484.1666 | 2.4 | 4 | -12 |
| 441 | 12355.5552 | 0.6 | 2 | -32 | 12381.1870 |  | 1 | 5 | 12557.7220 |  | 1 | -71 | 12590.5827 | 1.4 | 3 | 1 |
| 440 | 12355.5804 |  | 1 | -33 | 12381.2114 |  | 1 | 26 | 12557.7387 |  | 1 | -71 | 12590.6088 |  | 1 | -13 |
| 505 | 12049.7801 | 0.7 | 3 | -67 | 12091.0938 | 1.2 | 3 | 35 | 12281.2372 | 0.9 | 2 | -64 | 12414.4453 | 2.2 | 3 | -6 |
| 515 | 12054.4498 |  | 1 | -72 | 12094.9037 | 0.9 | 2 | 55 | 12284.4617 |  | 1 | -50 | 12415.5190 | 2.4 | 2 | -17 |
| 514 | 12142.1490 | 0.5 | 3 | -66 | 12184.5080* | 1.3 | 3 | 53 | 12373.5929 | 1.2 | 3 | -57 | 12492.3335 | 4.8 | 3 | 3 |
| 524 | 12179.6363 | 2.9 | 2 | -39 | 12218.3625 | 0.6 | 4 | 51 |  |  |  |  | 12509.8594 | 0.3 | 4 | 6 |
| 523 | 12209.3119 | 0.2 | 2 | -61 | 12248.1364* | 3.5 | 4 | 31 | 12437.0527 | 8.8 | 2 | -72 | 12541.1461 | 2.0 | 4 | 6 |
| 533 | 12312.8147 | 2.5 | 2 | -45 | 12345.2845 | 1.0 | 4 | 43 | 12529.1357 |  | 1 | -56 | 12599.2993 | 1.2 | 4 | -4 |
| 532 | 12315.5846 | 0.9 | 4 | -42 | 12348.6574 | 0.9 | 3 | 44 | 12532.9207 |  | 1 | -74 | 12604.4635 | 2.6 | 2 | 10 |
| 542 | 12474.0947 | 2.3 | 3 | -16 | 12500.1603 | 0.7 | 5 | 27 |  |  |  |  | 12707.9663 | 0.8 | 2 | 6 |
| 541 | 12474.3001 | 1.8 | 3 | -19 | 12500.3789 | 0.3 | 3 | 6 | 12677.2482 | 0.8 | 2 | -64 | 12708.2345 | 0.8 | 2 | 6 |
| 551 |  |  |  |  | 12687.7762 |  | 1 | 18 | 12859.5917 |  | 1 | -114 | 12840.7543 |  | 1 | 63 |
| 550 | 12667.5444 |  | 1 | -3 | 12687.7377 | 22.3 | 2 | -6 | 12859.6355 | 1.8 | 2 | -133 | 12840.7831 |  | 1 | 81 |
| 606 | 12165.6013 | 2.9 | 2 | -58 | 12207.2096 | 1.3 | 2 | 62 | 12397.8354 |  | 1 | -66 | 12528.2089 |  | 1 | 0 |
| 616 | 12168.2798 | 0.7 | 2 | -51 | 12209.2569 | 1.4 | 2 | 57 | 12398.7840 | 0.3 | 2 | -57 | 12528.6561 |  | 1 | -3 |
| 615 | 12286.2147 |  | 1 | -53 | 12327.8973 | 0.9 | 3 | 74 |  |  |  |  | 12629.2578 | 1.1 | 2 | 14 |
| 625 | 12314.0449 | 1.0 | 4 | -42 | 12352.4397* |  | 1 | 65 | 12540.2967 |  | 1 | -64 | 12636.5418 | 0.9 | 4 | 3 |
| 624 | 12362.8531 | 2.7 | 3 | -57 | 12403.5162 | 0.9 | 3 | 53 |  |  |  |  | 12691.8711 |  | 1 | 19 |
| 634 | 12453.6053 |  | 1 | -26 | 12486.9549* | 0.9 | 4 | 46 | 12672.3405 | 1.5 | 2 | -64 | 12738.3202 | 0.7 | 3 | 15 |
| 633 | 12461.4774 | 3.8 | 2 | -33 | 12496.1710 | 0.4 | 4 | 50 |  |  |  |  | 12751.6323 | 2.4 | 2 | 24 |
| 643 | 12616.0833 |  | 1 | -9 | 12641.9333 | 0.9 | 4 | 24 | 12820.6292 | 0.9 | 3 | -63 | 12849.1013* | 3.3 | 3 | 13 |
| 642 |  |  |  |  | 12643.7077 | 1.2 | 3 | 30 | 12821.2603 |  | 1 | -62 | 12850.2561 | 1.0 | 2 | 11 |
| 652 | 12810.3613 | 0.2 | 2 | 15 | 12831.8036 | 4.4 | 2 | 41 | 13005.0665 | 0.7 | 4 | -45 | 12981.5745 |  | 1 | 88 |
| 651 |  |  |  |  | 12831.7117 | 3.2 | 2 | 44 |  |  |  |  | 12981.7966 |  | 1 | 93 |
| 661 |  |  |  |  | 13042.8409 |  | 1 | 5 | 13209.1990 |  |  | -99 | 13145.9954 |  | 1 | 153 |
| 660 |  |  |  |  | 13042.8467 |  | 1 | 10 | 13209.2157 | 14.4 | 2 | -82 | 13145.9330 |  | 1 | 151 |
| 707 | 12297.8729 | 2.6 | 2 | -46 | 12339.8791 | 0.1 | 2 | 66 | 12529.9024 |  | 1 | -68 |  |  |  |  |
| 717 | 12299.5297 |  | 1 | -43 | 12341.0752 | 1.1 | 3 | 67 | 12531.5042 |  | 1 | -58 | 12659.1459 |  | 1 | -8 |
| 716 | 12448.3318 | 1.2 | 2 | -34 | 12489.9225 | 0.6 | 2 | 84 | 12680.6802 |  | 1 | -54 | 12782.6117 |  | 1 | 26 |
| 726 | 12467.7635 | 9.9 | 2 | 3 | 12506.9445 | 1.8 | 3 | 77 | 12694.1789 |  | 1 | -48 | 12788.3338 | 0.4 | 2 | 20 |
| 725 | 12542.2745 |  | 1 | -28 | 12582.3595 | 1.2 | 3 | 73 | 12772.3856 |  | 1 | -55 | 12864.7974 | 0.6 | 2 | 32 |
| 735 | 12616.6291 | 4.3 | 2 | -3 | 12650.4771 | 1.6 | 4 | 41 |  |  |  |  | 12898.8393 | 1.4 | 3 | 24 |
| 734 | 12634.0467 |  | 1 | -32 | 12670.8410 |  | 1 | 47 | 12859.8783 |  | 1 | -62 | 12925.8291* | 1.2 | 2 | 40 |
| 744 | 12779.9772 |  | 1 | -2 | 12811.6574 | 2.3 | 5 | 37 | 12987.8603 | 1.5 | 2 | -56 | 13013.2940 | 0.9 | 2 | 99 |
| 743 | 12785.0786 | 3.7 | 3 | 16 | 12811.5067 | 1.2 | 2 | 29 | 12989.6870 | 3.2 | 2 | -60 | 13017.805 | 2.7 | 4 | 65 |
| 753 |  |  |  |  | 12999.8777 | 1.3 | 2 | 47 |  |  |  |  | 13145.5457 | 1.6 | 2 | 99 |
| 752 | 12976.9858 |  | 1 | 22 | 12999.3658 | 2.0 | 2 | 55 | 13172.0896 | 4.2 | 2 | -112 | 13146.4573* |  | 1 | 107 |
| 762 |  |  |  |  | 13210.8123 | 0.8 | 3 | 3 |  |  |  |  | 13311.7418 |  | 1 | 179 |
| 761 |  |  |  |  | 13210.8224 | 16.8 | 2 | 22 |  |  |  |  | 13312.4085 |  | 1 | 133 |

Table 2 (continued)

| $J K_{a} K_{c}$ | (230) |  |  |  | (131) |  |  |  | (032) |  |  |  | (310) |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $E_{\text {obs }}\left(\mathrm{cm}^{-1}\right)$ | $\sigma$ | $N$ | $\Delta$ | $E_{\text {obs }}\left(\mathrm{cm}^{-1}\right)$ | $\sigma$ | $N$ | $\Delta$ | $E_{\text {obs }}\left(\mathrm{cm}^{-1}\right)$ | $\sigma$ | $N$ | $\Delta$ | $E_{\text {obs }}\left(\mathrm{cm}^{-1}\right)$ | $\sigma$ | $N$ | $\Delta$ |
| 770 |  |  |  |  |  |  |  |  | 13604.5321 |  | 1 | -36 | 13437.1810 |  | 1 | 257 |
| 808 | 12446.9919 |  | 1 | -32 | 12489.3172 |  | 1 | 77 |  |  |  |  | 12806.3779 |  | 1 | -9 |
| 818 | 12448.1633 | 3.5 | 2 | -23 | 12490.4034 | 0.8 | 2 | 80 |  |  |  |  | 12808.0558 |  | 1 | -4 |
| 817 | 12626.9563 | 8.3 | 2 | -28 | 12668.4974 | 0.9 | 3 | 84 |  |  |  |  | 12952.0877 |  | 1 | 124 |
| 827 | 12641.5210 | 0.1 | 2 | 31 |  |  |  |  | 12865.4547 |  | 1 | -44 | 12952.6148 | 0.2 | 2 | 16 |
| 826 | 12742.5132 |  | 1 | -58 | 12783.3694 | 0.2 | 4 | 68 |  |  |  |  | 13056.9875 |  | 1 | 32 |
| 836 | 12799.8827 |  | 1 | 5 | 12837.7298 | 2.5 | 2 | 41 |  |  |  |  | 13081.6550 | 0.8 | 5 | 42 |
| 835 |  |  |  |  | 12874.3217 | 0.6 | 3 | 52 |  |  |  |  | 13125.6560 | 0.8 | 3 | 52 |
| 845 | 12973.5317 | 1.5 | 2 | 16 | 13001.5305 | 0.1 | 2 | 40 | 13178.5014 |  | 1 | -59 | 13201.0502 |  | 1 | 48 |
| 844 |  |  |  |  | 13004.1845 | 1.3 | 3 | 23 | 13192.6441 | 3.7 | 2 | 50 | 13211.7693 |  | 1 | 102 |
| 854 | 13166.7002 |  | 1 | 45 | 13182.6206 |  | 1 | -32 |  |  |  |  | 13331.9172 |  | 1 | 85 |
| 853 |  |  |  |  | 13190.3297 |  | 1 | 70 |  |  |  |  |  |  |  |  |
| 863 |  |  |  |  | 13402.3285 | 0.3 | 2 | 0 | 13570.5118 |  | 1 | -106 | 13501.0595 |  | 1 | 201 |
| 862 |  |  |  |  | 13402.2562 |  | 1 | 1 |  |  |  |  | 13501.7761 |  | 1 | 175 |
| 872 | 13709.3012 |  | 1 | 408 |  |  |  |  | 13798.7141 |  | 1 | -45 | 13938.9548 |  | 1 | 189 |
| 871 |  |  |  |  | 13710.3773 |  | 1 | 280 |  |  |  |  |  |  |  |  |
| 881 |  |  |  |  |  |  |  |  |  |  |  |  | 14045.2336 |  | 1 | 410 |
| 880 |  |  |  |  | 13792.5572 |  | 1 | -221 |  |  |  |  |  |  |  |  |
| 909 |  |  |  |  | 12655.7461 | 1.8 | 2 | 80 |  |  |  |  | 12972.4938 | 0.6 | 2 | -9 |
| 919 |  |  |  |  | 12660.2612 |  | 1 | 95 |  |  |  |  | 12970.2791 |  | 1 | -11 |
| 918 | 12821.4954 |  | 1 | -6 | 12863.3858 |  | 1 | 107 | 13049.8335 | 4.6 | 2 | -75 | 13137.8108 |  | 1 | 31 |
| 928 |  |  |  |  | 12863.6025 | 3.3 | 2 | 60 |  |  |  |  |  |  |  |  |
| 927 | 12962.1370 |  | 1 | -21 | 13010.0686 |  | 1 | 76 |  |  |  |  | 13267.8167 |  | 1 | 47 |
| 937 | 13002.7670 |  | 1 | -502 | 13043.4827 | 0.3 | 2 | 54 | 13232.4397 |  | 1 | 13 | 13275.2832 | 0.6 | 3 | 24 |
| 936 |  |  |  |  | 13100.4850 |  | 1 | 57 |  |  |  |  | 13348.5340 | 4.2 | 2 | 50 |
| 946 |  |  |  |  | 13214.5020 |  | 1 | 42 | 13409.6887 |  | 1 | 59 | 13413.6417 |  | 1 | 92 |
| 945 | 13187.2280 |  | 1 | -41 | 13221.3552 |  | 1 | -3 | 13411.7184 |  | 1 | 35 | 13432.0821 |  | 1 | 56 |
| 955 |  |  |  |  | 13398.8506 |  | 1 | -11 |  |  |  |  |  |  |  |  |
| 954 |  |  |  |  | 13401.3779 |  | 1 | 49 |  |  |  |  | 13547.6252 |  | 1 | 119 |
| 964 |  |  |  |  | 13616.5652 |  | 1 | 3 |  |  |  |  |  |  |  |  |
| 963 | 13553.4872 |  | 1 | 119 | 13617.0494 |  | 1 | -4 |  |  |  |  |  |  |  |  |
| 973 |  |  |  |  | 13926.1148 |  | 1 | 159 |  |  |  |  |  |  |  |  |
| 972 |  |  |  |  |  |  |  |  |  |  |  |  | 13843.1461 |  | 1 | 298 |
| 982 |  |  |  |  | 14005.9484 |  | 1 | -243 |  |  |  |  |  |  |  |  |
| 10010 |  |  |  |  | 12839.9709 |  | 1 | 91 |  |  |  |  | 13417.7731 |  | 1 | 19 |
| 10110 |  |  |  |  |  |  |  |  |  |  |  |  | 13152.0965 |  | 1 | -19 |
| 1019 |  |  |  |  | 13076.2652 |  | 1 | 130 |  |  |  |  | 13339.6632 |  | 1 | -116 |
| 1029 |  |  |  |  | 13072.5030 |  | 1 | 64 |  |  |  |  | 13337.3548 | 1.1 | 3 | 29 |
| 1028 |  |  |  |  | 13246.4070 |  | 1 | 102 |  |  |  |  |  |  |  |  |
| 1038 |  |  |  |  |  |  |  |  | 13456.8546 |  | 1 | -60 | 13499.0790 | 1.2 | 2 | 24 |
| 1047 |  |  |  |  |  |  |  |  | 13648.3722 | 1.6 | 2 | 81 | 13641.3974 |  | 1 | 88 |
| 1046 |  |  |  |  | 13470.2890 |  | 1 | 43 |  |  |  |  |  |  |  |  |
| 1056 |  |  |  |  |  |  |  |  |  |  |  |  | 13784.5277 |  | 1 | 135 |
| 1055 |  |  |  |  |  |  |  |  |  |  |  |  | 13785.0728 |  | 1 | 116 |
| 1065 |  |  |  |  |  |  |  |  |  |  |  |  | 13949.6191 |  | 1 | 246 |
| 1074 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 11011 |  |  |  |  |  |  |  |  |  |  |  |  | 13350.6102 |  | 1 | -43 |
| 11111 |  |  |  |  | 13036.8706 |  | 1 | 73 |  |  |  |  |  |  |  |  |
| 11210 |  |  |  |  | 13298.1974 |  | 1 | 88 |  |  |  |  |  |  |  |  |
| 11210 |  |  |  |  | 13298.1974 |  | 1 | 88 |  |  |  |  |  |  |  |  |
| 1129 |  |  |  |  |  |  |  |  |  |  |  |  | 13736.1928 |  | 1 | 61 |
| 1139 |  |  |  |  |  |  |  |  |  |  |  |  | 13727.0218 |  | 1 | 4 |
| 1138 | 13576.5609 |  | 1 | 12 |  |  |  |  |  |  |  |  |  |  |  |  |
| 1148 |  |  |  |  | 13705.5870 |  | 1 | 10 | 13897.0961 |  | 1 | 43 |  |  |  |  |
| 1156 |  |  |  |  |  |  |  |  |  |  |  |  | 14322.9226 |  | 1 | 137 |
| 1165 |  |  |  |  |  |  |  |  |  |  |  |  | 14471.5433 |  | 1 | 149 |
| 1175 |  |  |  |  | 14426.6719 |  | 1 | 63 |  |  |  |  |  |  |  |  |
| 12012 |  |  |  |  | 13253.1916 |  | 1 | 82 |  |  |  |  |  |  |  |  |
| 12310 |  |  |  |  |  |  |  |  | 13965.5951 |  | 1 | -94 | 14255.6363 |  | 1 | 58 |
| 1248 |  |  |  |  | 14047.9220 |  | 1 | 85 |  |  |  |  |  |  |  |  |
| 1258 |  |  |  |  |  |  |  |  |  |  |  |  | 14316.5803 |  | 1 | 110 |

[^2]Table 3
Energy levels of the (211), (112) and (013) vibrational states of $\mathrm{H}_{2}{ }^{18} \mathrm{O}$

| ${ }_{J} K_{a} K_{c}$ | (211) |  |  |  | (112) |  |  |  | (013) |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $E_{\text {obs }}\left(\mathrm{cm}^{-1}\right)$ | $\sigma$ | $N$ | 4 | $E_{\text {obs }},\left(\mathrm{cm}^{-1}\right)$ | $\sigma$ | $N$ | $\Delta$ | $E_{\text {obs }},\left(\mathrm{cm}^{-1}\right)$ | $\sigma$ | $N$ | $\Delta$ |
| 000 | 12116.8148 |  | 1 | -21 | 12372.7045 |  | 1 | 42 | 12520.1234 |  | 1 | 56 |
| 101 | 12139.4429 |  |  |  | 12395.5226 | 0.1 | 2 | 46 | 12543.2309 | 0.0 | 2 | 63 |
| 111 | 12152.9458 |  | 1 | -33 | 12408.7973 | 0.9 | 3 | 41 | 12555.3766 | 2.7 | 2 | 69 |
| 110 | 12158.5055 |  |  |  | 12414.3831 |  | 1 | 43 | 12561.0828 |  | 1 | 72 |
| 202 | 12184.6750 |  | 1 | -24 | 12439.7095 | 1.0 | 2 | 46 | 12587.8106 |  | 1 | 58 |
| 212 | 12192.9163 |  | 1 | -34 | 12448.8445 | 0.6 | 3 | 43 | 12595.8891 | 0.4 | 2 | 64 |
| 211 | 12209.5335 |  | 1 | -50 | 12465.5716 | 0.4 | 3 | 46 | 12612.9928 |  | 1 | 80 |
| 221 | 12249.3643 | 0.8 | 2 | -27 | 12505.3433 | 1.1 | 3 | 36 | 12649.0258 | 1.2 | 2 | 66 |
| 220 | 12250.7607 | 3.7 | 2 | -33 | 12506.7552 | 0.7 | 2 | 53 | 12650.6133 | 1.3 | 2 | 64 |
| 303 | 12247.2810 | 1.4 | 2 | -38 | 12502.9510 | 0.5 | 3 | 47 | 12651.1968 | 0.3 | 2 | 73 |
| 313 | 12252.1098 | 0.7 | 3 | -28 | 12508.0806 | 0.7 | 2 | 30 | 12655.7295 | 1.7 | 2 | 63 |
| 312 | 12284.9474 | 0.5 | 3 | -19 | 12541.2109 | 0.0 | 2 | 47 | 12689.5440 | 0.0 | 2 | 67 |
| 322 | 12317.6522 | 1.4 | 2 | -22 | 12573.7974 | 0.5 | 5 | 52 | 12718.4472 | 0.8 | 3 | 67 |
| 321 | 12324.1128 | 0.8 | 5 | -33 | 12580.2840 | 3.5 | 3 | 48 | 12725.6516 | 0.6 | 4 | 81 |
| 331 | 12397.4688 | 4.0 | 2 | -15 | 12653.6167 | 1.4 | 4 | 45 | 12792.3556 | 0.1 | 4 | 68 |
| 330 | 12397.6976 |  | 1 | -18 | 12653.6739 | 0.7 | 4 | 59 | 12792.6474 | 1.1 | 2 | 66 |
| 404 | 12327.5791 | 0.1 | 2 | -21 | 12583.5143 | 0.7 | 2 | 31 | 12731.9896 |  | , | 62 |
| 414 | 12329.8604 | 0.7 | 2 | -23 | 12585.8110 | 1.1 | 4 | 46 | 12734.1433 |  | 1 | 48 |
| 413 | 12383.0613 | 3.0 | 2 | -9 | 12639.6848 | 0.9 | 3 | 38 | 12788.8539 | 1.4 | 3 | 70 |
| 423 | 12407.5054 |  | 1 | -30 | 12663.8254 | 6.0 | 5 | 50 | 12809.5788 |  | 1 | 84 |
| 422 | 12424.3363 | 1.4 | 4 | -9 | 12680.7516 | 0.9 | 5 | 57 | 12828.0034 |  | 1 | 65 |
| 432 | 12490.8327 | 0.7 | 3 | -12 | 12747.1377 | 1.1 | 4 | 61 | 12887.7532 | 0.9 | 4 | 71 |
| 431 | 12492.3687 | 0.2 | 3 | -9 | 12748.5089 | 1.3 | 5 | 49 | 12889.6457 | 0.8 | 3 | 71 |
| 441 | 12597.3561 | 0.9 | 2 | -13 | 12852.8830 | 3.0 | 4 | 73 | 12985.1955 | 0.6 | 2 | 82 |
| 440 | 12597.3864 | 0.9 | 3 | -2 | 12852.8797 | 1.8 | 3 | 70 | 12985.2438 | 0.9 | 3 | 71 |
| 505 | 12424.6186 | 0.9 | 2 | -36 | 12680.0950 |  | 2 | -1 | 12829.5228 | 0.9 | 3 | 71 |
| 515 | 12425.5860 | 0.4 | 2 | -20 | 12681.4688 |  | 1 | 34 | 12830.6608 |  | , | 58 |
| 514 | 12501.3453 |  | 2 | -5 | 12758.6394 | 1.5 | 4 | 59 | 12908.2655 | 0.5 | 3 | 70 |
| 524 | 12518.1262 | 0.9 | 2 | -7 | 12774.5020 | 0.8 | 4 | 61 | 12921.3754 | 0.5 | 3 | 67 |
| 523 | 12550.7400 | 1.2 | 3 | -16 | 12807.3394 | 0.9 | 4 | 62 | 12956.6192 | 0.8 | 3 | 87 |
| 533 | 12607.3117 | 1.0 | 4 | -3 | 12864.1157 | 1.4 | 4 | 52 | 13006.5679 | 1.0 | 3 | 75 |
| 532 | 12612.8595 | 1.6 | 6 | 2 | 12869.3372 | 1.2 | 5 | 64 | 13013.1672 | 0.9 | 4 | 68 |
| 542 | 12714.5646 | 0.3 | 3 | 7 | 12970.1885 | 0.1 | 2 | 76 | 13108.8782 | 7.1 | 4 | 81 |
| 541 | 12714.8399 | 1.1 | 3 | -13 | 12970.2579 | 1.7 | 4 | 73 | 13109.1026 | 2.2 | 2 | 93 |
| 551 | 12848.2381 |  | 1 | 28 | 13098.8304 | 0.3 | 2 | 70 | 13225.9351 |  | 1 | 59 |
| 550 | 12848.2412 |  | 1 | 31 | 13098.6631 | 0.5 | 3 | 75 | 13225.9507 |  | 1 | 69 |
| 606 | 12538.4747 | 2.4 | 2 | -19 | 12794.0514 |  | 1 | 41 | 12944.0103 | 0.4 | 2 | 56 |
| 616 | 12538.9016 | 0.4 | 2 | -20 | 12794.6744 | 0.1 | 3 | 50 | 12943.9995 | 0.6 | 3 | 52 |
| 615 | 12641.8862 | 0.5 | 3 | 12 | 12895.5801 | 0.5 | 3 | 64 | 13045.2393 | 0.6 | 4 | 67 |
| 625 | 12649.5880 | 0.3 | 3 | 7 | 12904.8393 | 0.7 | 4 | 67 | 13052.8860 | 0.5 | 3 | 69 |
| 624 | 12701.5408 | 1.3 | 5 | 10 | 12959.1435 | 0.9 | 3 | 66 | 13109.3285 |  | 1 | 53 |
| 634 | 12746.2170 | 0.6 | 5 | 3 | 13002.5358 | 1.5 | 4 | -5 | 13148.0772 | 2.9 | 2 | 79 |
| 633 | 12760.3973 | 2.2 | 5 | 16 | 13017.2924 | 0.9 | 4 | 71 | 13164.3591 | 1.7 | 4 | 76 |
| 643 | 12855.4210 | 0.6 | 4 | 21 | 13111.2771 | 0.8 | 4 | 81 | 13253.6598 | 1.3 | 3 | 99 |
| 642 | 12856.6935 | 1.6 | 6 | 19 | 13111.9185 |  | 1 | 74 | 13254.7144 | 8.3 | 3 | 92 |
| 652 | 12989.2226 | 1.6 | 2 | 35 | 13239.2470 | 0.1 | 2 | 72 | 13368.0645 |  | 1 | 70 |
| 651 | 12989.2621 | 0.5 | 3 | 48 | 13238.5876 | 0.4 | 2 | 74 | 13368.1289* | 0.1 | 2 | 72 |
| 661 | 13151.2170 |  | 1 | 98 | 13402.5737 |  | 1 | 125 |  |  |  |  |
| 660 | 13151.2185 |  | 1 | 92 |  |  |  |  | 13512.4530** |  | 1 | 76 |
| 707 | 12669.3197 |  | 1 | -21 | 12924.9560 | 8.0 | 2 | 61 | 13075.6053 | 0.0 | 2 | 45 |
| 717 | 12669.7741 | 0.2 | 2 | -14 | 12925.3279 | 1.6 | 2 | 49 | 13075.6737 |  | 1 | 45 |
| 716 | 12794.1463 |  | 1 | 12 | 13048.9659 | 0.2 | 3 | 69 | 13198.5454 | 0.7 | 4 | 61 |
| 726 | 12795.7346 | 0.7 | 4 | 5 | 13054.0234 | 0.8 | 3 | 72 | 13204.4582 | 0.1 | 2 | 75 |
| 725 | 12874.3542 | 2.5 | 3 | 17 | 13132.2504 | 1.4 | 4 | 31 | 13283.4531 | 0.8 | 2 | 67 |
| 735 | 12906.5845 |  | 1 | 13 | 13164.6163 | 1.8 | 3 | 73 | 13310.4632* | 1.9 | 4 | 96 |
| 734 | 12935.0374 | 1.1 | 4 | 32 | 13191.1224 | 0.5 | 2 | 68 | 13342.8092 | 1.4 | 3 | 76 |
| 744 | 13019.6535 | 0.6 | 4 | 34 | 13275.7826 |  | 1 | 90 | 13421.6602 | 1.1 | 2 | 102 |
| 743 | 13023.7989 | 0.7 | 4 | 29 | 13278.5654 | 1.1 | 3 | 78 | 13425.3618 |  | 1 | 93 |

Note. $N$ is the number of lines used for the upper energy level determination, $\sigma$ denotes the corresponding standard deviation calculated for energies determined from more than one transition in $10^{-3} \mathrm{~cm}^{-1}$ units and $\Delta$ is the deviation of the observed levels from their calculated values [19] in 10 ${ }^{-3} \mathrm{~cm}^{-1}$. Levels marked by * and + are in disagreement with those reported in Ref. [5] and Ref. [7], respectively. For completeness, the energy values of the [101] and [110] levels of the (211) vibrational state are reproduced from Ref. [5] as the corresponding transitions are saturated in the ICLAS spectrum.

Table 3 (continued)

| $J K_{a} K_{c}$ | (211) |  |  |  | (112) |  |  |  | (013) |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $E_{\text {obs }},\left(\mathrm{cm}^{-1}\right)$ | $\sigma$ | $N$ | $\triangle$ | $E_{\text {obs }},\left(\mathrm{cm}^{-1}\right)$ | $\sigma$ | $N$ | $\triangle$ | $E_{\mathrm{obs}},\left(\mathrm{cm}^{-1}\right)$ | $\sigma$ | $N$ | $\Delta$ |
| 753 | 13153.8514 | 0.8 | 2 | 54 | 13404.3509 |  | 1 | 80 |  |  |  |  |
| 752 | 13154.0374 | 2.3 | 5 | 66 | 13402.6550 | 4.4 | 2 | 82 | 13534.3497 |  | 1 | 69 |
| 762 | 13316.6740 |  | 1 | 122 | 13569.4223 |  | 1 | 160 | 13679.0913 | 0.1 | 2 | 80 |
| 761 | 13316.6793 | 7.1 | 2 | 110 | 13569.3840 |  | 1 | 122 |  |  |  |  |
| 771 | 13437.1064 | 1.0 | 2 | -2 |  |  |  |  |  |  |  |  |
| 770 | 13437.1078 |  | 1 | -1 | 13748.6055 |  | 1 | 175 |  |  |  |  |
| 808 | 12817.5826 |  | 1 | -17 | 13072.9422* | 2.8 | 2 | 49 | 13224.4051 | 2.5 | 3 | 40 |
| 818 | 12816.5635 |  | 1 | -27 | 13071.7020* |  | 1 | 25 | 13224.3890 |  | 1 | 32 |
| 817 | 12961.8256 | 1.3 | 3 | 14 | 13218.6478 | 0.1 | 2 | 73 | 13368.1674 | 0.2 | 3 | 52 |
| 827 | 12963.2691 | 0.9 | 4 | 8 | 13221.7287 | 2.1 | 4 | 77 | 13368.8053* | 1.4 | 3 | 47 |
| 826 | 13066.4118 | 0.8 | 3 | 27 | 13324.4956 |  | 1 | 80 | 13476.0040 | 0.3 | 3 | 59 |
| 836 | 13087.7043 | 0.9 | 2 | 14 | 13347.6871* | 0.8 | 4 | 92 | 13494.7185 |  | 1 | 77 |
| 835 | 13135.2579 | 0.4 | 2 | 47 | 13396.0062 | 0.2 | 2 | 91 | 13546.6099 |  | 1 | 47 |
| 845 | 13206.5792 | 1.4 | 3 | 44 | 13463.0104 | 1.9 | 3 | 93 | 13612.6676 |  | 1 | 99 |
| 844 | 13217.2436 | 2.7 | 4 | 37 | 13470.6823 |  | 1 | 70 | 13622.6055 |  | 1 | 83 |
| 854 | 13342.0742 | 0.7 | 2 | 71 |  |  |  |  | 13723.6345 |  | 1 | 49 |
| 853 | 13342.7903 | 0.4 | 3 | 82 | 13590.5856 |  | 1 | 76 | 13724.9210 | 0.1 | 2 | 68 |
| 863 | 13505.6176 |  | 1 | 141 | 13759.8859 |  | 1 | 144 |  |  |  |  |
| 862 | 13505.6701 | 0.9 | 3 | 128 | 13759.7863 |  | 1 | 140 | 13869.5479 |  | 1 | 64 |
| 871 | 13628.1983 | 0.5 | 3 | -9 |  |  |  |  | 14032.5553 |  | 1 | 91 |
| 880 |  |  |  |  |  |  |  |  | 14213.5941 |  | 1 | 85 |
| 909 | 12981.1403 | 1.3 | 3 | -25 | 13237.0279 |  | 1 | 31 | 13390.2746 |  | 1 | 25 |
| 919 | 12981.8952 | 1.1 | 3 | -30 | 13239.2860* |  | 1 | 8 | 13390.2799 |  | 1 | 23 |
| 918 | 13147.9845 | 0.5 | 4 | 18 | 13404.0812 | 1.0 | 3 | 70 | 13553.6585 |  | 1 | 60 |
| 928 | 13148.1141 | 0.1 | 2 | 17 |  |  |  |  | 13554.7772 |  | 1 | 45 |
| 927 | 13282.5249 | 1.7 | 2 | 40 | 13533.8363 |  | 1 | 76 | 13684.8437 |  | 1 | 52 |
| 937 | 13288.0590 | 2.9 | 4 | 17 | 13538.1441 | 2.7 | 2 | 63 | 13701.5649 |  | 1 | 95 |
| 936 | 13358.4250 | 1.5 | 3 | 58 | 13621.0636 | 1.2 | 2 | 80 | 13773.4009 |  | 1 | 88 |
| 946 | 13416.4575 | 1.2 | 4 | 60 | 13672.1061 | 1.5 | 2 | 89 | 13826.2871 |  | 1 | 107 |
| 945 | 13437.8607 | 1.6 | 3 | 53 | 13685.3778 |  | 1 | 47 | 13847.6668 |  | 1 | 88 |
| 955 | 13553.6063 | 1.0 | 3 | 77 | 13806.3401 |  | 1 | 99 | 13936.6731 |  | 1 | 49 |
| 954 | 13556.7241 | 2.9 | 3 | 88 | 13802.2726 |  | 1 | 69 |  |  |  |  |
| 964 | 13717.9544 | 1.3 | 2 | 161 | 13974.1618 |  | 1 | 159 | 14084.0041 |  | 1 | 54 |
| 963 |  |  |  |  | 13973.6923 |  | 1 | 144 |  |  |  |  |
| 973 | 13842.3564 | 4.6 | 2 | -22 |  |  |  |  |  |  |  |  |
| 972 |  |  |  |  | 14152.5285 |  | 1 | 203 |  |  |  |  |
| 10010 | 13163.2881 |  | 1 | -56 |  |  |  |  | 13573.3523 |  | 1 | -6 |
| 10110 | 13163.2545 |  | 1 | -60 | 13418.2785 |  | 1 | 34 | 13573.3881 |  | 1 | 26 |
| 1019 | 13346.0860 | 1.7 | 3 | 28 |  |  |  |  | 13757.3077 | 6.5 | 2 | 47 |
| 1029 | 13349.5964 | 2.5 | 3 | 37 | 13604.8239 | 0.4 | 2 | 72 | 13757.5682 |  | 1 | 37 |
| 1028 | 13505.1904 | 0.2 | 2 | 27 |  |  |  |  | 13909.2421 |  | 1 | 27 |
| 1038 | 13507.2730 |  | 1 | -4 | 13760.2684 |  | 1 | -84 | 13911.6000 |  | 1 | 19 |
| 1037 | 13600.5358 | 0.0 | 3 | 38 |  |  |  |  | 14019.6143 |  | 1 | 76 |
| 1047 | 13646.4968 |  | 1 | 51 | 13902.1375 | 4.5 | 2 | 86 |  |  |  |  |
| 1046 | 13684.9107 | 1.3 | 3 | 52 |  |  |  |  | 14099.1813 |  | 1 | 61 |
| 1056 |  |  |  |  | 14041.5060 |  | 1 | 104 |  |  |  |  |
| 1055 | 13794.5063 | 1.4 | 3 | 108 |  |  |  |  |  |  |  |  |
| 1065 | 13953.3780 |  | 1 | 60 | 14212.7225 |  | 1 | 154 |  |  |  |  |
| 1064 | 13954.0127 | 2.5 | 2 | 156 |  |  |  |  |  |  |  |  |
| 1073 | 14079.3817 |  | 1 | -28 |  |  |  |  |  |  |  |  |
| 11011 | 13362.0990 | 2.0 | 2 | -55 | 13617.0849 |  | 1 | 25 | 13773.7005+ |  | 1 | -6 |
| 11111 | 13362.0980 | 3.6 | 2 | -63 |  |  |  |  | 13773.5158 |  | 1 | -17 |
| 11210 | 13567.1425 |  | 1 | 27 |  |  |  |  | 13977.4415 |  | 1 | 20 |
| 1129 | 13740.0941 |  | 1 | 17 | 14000.1303 |  | 1 | 72 | 14149.4297 |  | 1 | 6 |
| 1139 | 13745.1607 |  | 1 | -4 |  |  |  |  | 14150.9266 |  | 1 | -1 |
| 1138 | 13862.7517 |  | 1 | 49 |  |  |  |  | 14282.6669 |  | 1 | 57 |
| 1148 | 13897.1372 |  | 1 | 42 |  |  |  |  |  |  |  |  |
| 1147 | 13957.1900 |  | 1 | 40 |  |  |  |  |  |  |  |  |
| 12012 | 13577.7683 |  | 1 | -69 |  |  |  |  | 13991.1324 |  | 1 | -32 |
| 12112 | 13577.7692 |  | 1 | -53 |  |  |  |  | 13989.8851 |  | 1 | -47 |
| 12111 | 13804.2716 | 0.8 | 2 | -1 |  |  |  |  | 14215.5582 |  | 1 | 71 |
| 12211 | 13804.2404 |  | 1 | -1 |  |  |  |  |  |  |  |  |
| 12210 | 13997.9066 | 6.9 | 3 | 8 |  |  |  |  | 14406.1591 |  | 1 | -13 |
|  |  |  |  |  |  |  |  |  |  | cont |  |  |

Table 3 (continued)

| $J K_{a} K_{c}$ | (211) |  |  |  | (112) |  |  |  | (013) |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $E_{\text {obs }},\left(\mathrm{cm}^{-1}\right)$ | $\sigma$ | $N$ | $\Delta$ | $E_{\text {obs }},\left(\mathrm{cm}^{-1}\right)$ | $\sigma$ | $N$ | $\Delta$ | $E_{\text {obs }},\left(\mathrm{cm}^{-1}\right)$ | $\sigma$ | $N$ | $\Delta$ |
| 12310 | 13998.7880 |  | 1 | 4 |  |  |  |  |  |  |  |  |
| 1239 | 14140.4631 |  | 1 | 37 |  |  |  |  |  |  |  |  |
| 1248 | 14249.0715 |  | 1 | 35 |  |  |  |  |  |  |  |  |
| 1257 | 14349.3577 |  | 1 | 109 |  |  |  |  |  |  |  |  |
| 13013 | 13810.2766 |  | 1 | -144 |  |  |  |  |  |  |  |  |
| 13113 | 13810.2767 | 0.3 | 2 | -142 |  |  |  |  | 14223.8492 |  | 1 | -110 |
| 13112 | 14057.0729 |  | 1 | -60 |  |  |  |  |  |  |  |  |
| 13212 | 14057.0930 |  | 1 | -8 |  |  |  |  | 14469.1323 |  | 1 | 0 |
| 13211 | 14271.0121 |  | 1 | -4 |  |  |  |  |  |  |  |  |
| 13311 | 14270.3987 |  | 1 | -11 |  |  |  |  |  |  |  |  |
| 13410 | 14452.1982 |  | 1 | 76 |  |  |  |  |  |  |  |  |
| 14014 | 14062.4019 |  | 1 | 71 |  |  |  |  |  |  |  |  |

Table 4
Energy levels of the (003), (023), (051), (061), (080), (090), (150), (160) and (221) vibrational states of $\mathrm{H}_{2}{ }^{18} \mathrm{O}$

| $J K_{a} K_{c}$ | $E_{\text {obs }}\left(\mathrm{cm}^{-1}\right)$ | $\sigma$ | $N$ | $\Delta$ |
| :---: | :---: | :---: | :---: | :---: |
| (003) |  |  |  |  |
| 12210 | 12848.7724 |  | 1 | -40 |
| (023) |  |  |  |  |
| 220 | 14157.3123 |  | 1 | 38 |
| 322 | 14225.4924 |  | 1 | 47 |
| (051) |  |  |  |  |
| 744 | 12480.8840 |  | 1 | 80 |
| 771 | 13329.7863 |  | 1 | -55 |
| 845 | 12685.2532 |  | 1 | 111 |
| 881 | 13865.8493 |  | 1 | 37 |
| 880 | 13865.8493 |  | 1 | 23 |
| 937 | 12641.2467 |  | 1 | 54 |
| 10110 | 13357.1153 | 1.2 | 2 | 23 |
| (061) |  |  |  |  |
| 817 | 13548.1584 |  | 1 | 38 |
| (080) |  |  |  |  |
| 937 | 12667.9783 |  | 1 | 48 |
| 1029 | 13359.0688 |  | 1 | 27 |
| (090) |  |  |  |  |
| 505 | 12832.1188 |  | 1 | -192 |
| (150) |  |  |  |  |
| 431 | 11733.7897 |  | 1 | 63 |
| 845 | 12601.8038 |  | 1 | 106 |
| 946 | 12807.4902 |  | 1 | 48 |
| 963 | 13425.2693 |  | 1 | 358 |
| (160) |  |  |  |  |
| 505 | 12691.9985 |  | 1 | 286 |
| (221) |  |  |  |  |
| 101 | 13635.1708+ |  | 1 | -61 |
| 111 | 13651.9814 |  | 1 | 238 |
| 221 | 13757.7727 |  | 1 | 213 |
| 322 | 13826.2276 |  | 1 | 240 |
| 331 | 13919.9622 |  | 1 | 222 |
| 413 | 13884.6231 |  | 1 | 266 |
| 515 | 13922.9622 |  | 1 | 250 |
| 717 | 14166.1557 | 1 | 2 | 240 |

Note. $N$ is the number of lines used for the upper energy level determination, $\sigma$ denotes the corresponding standard deviation calculated for energies determined from more than one transition in $10^{-3} \mathrm{~cm}^{-1}$ units and $\Delta$ is the deviation of the observed levels from their calculated values in $10^{-3} \mathrm{~cm}^{-1}$. The level marked by + is in disagreement with that reported in Ref. [7].
energy. Lines such as components of unresolved blends, very weak and saturated ones can have significant errors in their positions and intensities and were then excluded from the energy level derivation.


Fig. 4. Difference of the observed and calculated values [19,20] for the energy levels of the (032) and (131) vibrational states (left hand) and (013) and (112) vibrational states (right hand).


Fig. 5. Difference of the observed and calculated values $[19,20]$ as a function of the quantity $\left(J+K_{a}-K_{c}+1\right)$ for the $J=7$ energy levels of seven $\left(v_{1}, v_{2}, \mathrm{v}_{3}\right)$ vibrational states which are indicated on the plot. The picture shows a systematic behavior of the (obs-calc) values which confirms the correctness of the assignment.

Table 5
Energy levels of the (013) and (301) vibrational states of $\mathrm{HD}^{18} \mathrm{O}$

| $J K_{a} K_{c}$ | $E_{\text {obs }}\left(\mathrm{cm}^{-1}\right)$ | $\sigma$ | $N$ | $\Delta$ |
| :---: | :---: | :---: | :---: | :---: |
| 013 |  |  |  |  |
| 101 | 11947.8669 |  | 1 | -275 |
| 111 | 11960.3465 |  | 1 | -274 |
| 110 | 11963.4779 |  | 1 | -270 |
| 202 | 11977.7918 |  | 1 | -275 |
| 212 | 11987.6654 | 1.2 | 2 | -270 |
| 211 | 11997.0345 | 0.6 | 2 | -275 |
| 221 | 12034.2836 | 0.6 | 2 | -263 |
| 220 | 12034.8079 |  | 1 | -254 |
| 303 | 12021.4542 | 2 | 2 | -278 |
| 313 | 12028.3240 | 0.1 | 2 | -273 |
| 312 | 12047.0032 |  | 1 | -263 |
| 322 | 12079.9039 | 0.3 | 2 | -266 |
| 321 | 12082.3922 | 0.1 | 2 | -260 |
| 331 | 12149.4939 |  | 1 | -247 |
| 330 | 12149.5496 |  | 1 | -245 |
| 404 | 12077.8014 | 0.2 | 2 | -276 |
| 414 | 12082.0315 | 1.2 | 2 | -272 |
| 413 | 12112.8108 | 2.4 | 2 | -276 |
| 423 | 12140.2983 | 0.6 | 2 | -267 |
| 422 | 12147.2165 |  | 1 | -269 |
| 432 | 12211.1231 |  | 1 | -249 |
| 431 | 12211.4906 |  | 1 | -251 |
| 441 | 12306.1611 |  | 1 | -223 |
| 440 | 12306.1781 |  | 1 | -210 |
| 505 | 12146.1217 |  | 1 | -276 |
| 515 | 12148.4794 | 1.2 | 2 | -273 |
| 514 | 12193.6768 |  | 1 | -282 |
| 524 | 12215.0951 | 2.2 | 2 | -277 |
| 523 | 12229.5501 |  | 1 | -301 |
| 533 | 12288.2583 |  | 1 | -255 |
| 542 | 12383.1043 |  | 1 | -209 |
| 541 | 12383.1031 |  | 1 | -251 |
| 550 | 12503.2945 |  | 1 | -198 |
| 606 | 12226.1949 |  | 1 | -269 |
| 616 | 12227.4086 |  | 1 | -278 |
| 615 | 12288.5150 |  | 1 | -280 |
| 625 | 12303.9000 | 1.8 | 2 | -274 |
| 624 | 12329.1196 |  | 1 | -280 |
| 633 | 12384.7966 |  | 1 | -242 |
| 643 | 12475.6095 |  | 1 | -249 |
| 642 | 12475.8264 |  | 1 | -233 |
| 660 | 12739.7016 |  | 1 | -163 |
| 716 | 12396.1233 | 0.5 | 2 | -285 |
| 726 | 12406.2501 | 0.3 | 2 | -277 |
| 725 | 12445.0876 |  | 1 | -290 |
| 735 | 12488.5281 |  | 1 | -181 |
| 744 | 12583.8275 |  | 1 | -246 |
| 808 | 12421.6895 |  | 1 | -313 |
| 818 | 12422.0186 | 4.6 | 2 | -278 |
| 817 | 12515.5715 |  | 1 | -289 |
| 827 | 12521.7392 | 1.3 | 2 | -276 |
| 826 | 12576.4503 |  | 1 | -280 |
| 836 | 12611.3738 |  | 1 | 230 |
| 835 | 12628.0996 |  | 1 | -275 |
| 845 | 12707.6957 |  | 1 | -241 |
| 844 | 12709.6839 |  | 1 | -253 |
| 909 | 12537.2998 |  | 1 | -308 |
| 919 | 12537.4709 |  | 1 | -272 |
| 918 | 12646.4341 |  | 1 | -292 |
| 928 | 12650.0989 |  | 1 | -88 |
| 937 | 12747.6041 |  | 1 | -288 |
| 936 | 12776.3991 |  | 1 | -304 |
| 10010 | 12664.8295 |  | 1 | -311 |

Table 5 (continued)

| $J K_{a} K_{c}$ | $E_{\text {obs }}\left(\mathrm{cm}^{-1}\right)$ | $\sigma$ | $N$ | $\Delta$ |
| :--- | :--- | :--- | :--- | :--- |
| 10110 | 12664.9153 |  | 1 | -287 |
| 1029 | 12790.7151 | 1 | -124 |  |
| 11011 | 12804.2833 | 1 | -313 |  |
| 11111 | 12804.3259 | 1 | -299 |  |
| 1138 | 13122.7762 | 1 | -25 |  |
| 12211 | 13107.8059 | 1 | -787 |  |
| 301 |  |  |  |  |
| 330 | 11746.5363 | 1 | -84 |  |

Note. $N$ is the number of lines used for the upper energy level determination, $\sigma$ denotes the corresponding standard deviation calculated for energies determined from more than one transition in $10^{-3} \mathrm{~cm}^{-1}$ units and $\Delta$ is the deviation of the observed levels from their calculated values in $10^{-3} \mathrm{~cm}^{-1}$.

Among the 315 levels determined by Bykov et al. [5], 309 are common with ours. However, seventeen of their levels (marked by * in Tables 2 and 3) deviate by more than $0.1 \mathrm{~cm}^{-1}$, some up to a few wavenumbers.

For the levels coinciding within $10^{-2} \mathrm{~cm}^{-1}$, the average value of the deviations and the corresponding rms are $-0.4 \times 10^{-3}$ and $3 \times 10^{-3} \mathrm{~cm}^{-1}$, respectively. Similarly, we identified in Ref. [7], six levels which have a deviation comprised between 0.1 and $0.3 \mathrm{~cm}^{-1}$ (they are marked by + in Tables 2 and 3 ).

Among the valuable information retrieved from the spectra, it is worth noticing that (i) the (032) state is detected for the first time and 64 of its levels could be determined, (ii) 69 levels of the (230) state were assigned in the ICLAS spectrum while only 10 of them were previously determined from Kitt Peak spectra [5], (iii) the band origins of the (230) and (310) could be experimentally determined.

As illustrated in Figs. 2-5, a good agreement is noted between the ICLAS and SP calculated spectra. According to the vibrational state, some systematic tendencies are observed for the deviations of the calculated energy levels from their experimental values (see Figs. 4 and 5), confirming the consistency of our assignments. Maximum values are on the order of $0.1 \mathrm{~cm}^{-1}$ but the average deviation is only $0.004 \mathrm{~cm}^{-1}$.

Table 5 lists the 70 energy levels determined for the $\mathrm{HD}^{18} \mathrm{O}$ isotopologue. The upper level energies were derived by adding the ground state energy values [3] to the observed transitions. Most of them belong to the (013) state which corresponds to the strongest band in this region.

## 4. Line intensities

In the considered spectral region, HITRAN provides only 164 transitions for $\mathrm{H}_{2}{ }^{18} \mathrm{O}$, all lying between 12400 and $12700 \mathrm{~cm}^{-1}$ and all having line strengths larger than $7 \times 10^{-26} \mathrm{~cm} /$ molecule, with a maximum intensity of $4.3 \times 10^{-24} \mathrm{~cm} /$ molecule. The histogram of the ratio of FTS line strengths [7] compared to the results of Schwenke and Partridge calculations $[19,20]$ is shown in Fig. 6. It shows a clear difference on the order of $25 \%$ on average,


Fig. 6. Histogram of the ratio of the $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ line strengths as reported by HITRAN in the $12400-12700 \mathrm{~cm}^{-1}$ region, by the intensity values calculated by Schwenke and Partridge [19,20].


Fig. 7. Ratio of the ICLAS line intensities by calculated [19,20] values versus the ICLAS intensity values. The lines in the hatched region are saturated in the ICLAS spectrum, resulting in an underestimation of their line strength.
the HITRAN values being larger than SP calculations. Note that the line list of Ref. [7] is the one adopted in the last version of the HITRAN database.

As illustrated in Fig. 7, a much more complete comparison ( 1623 lines) can be performed between the ICLAS line intensities of $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ with SP predictions $[19,20]$. As a consequence of saturation effects in our spectra, only lines with intensities lower than the intensity cutoff fixed at $5 \times 10^{-25} \mathrm{~cm} /$ molecule have to be considered. The ICLAS/SP intensity ratio falls in the $[0.94,1.56]$ interval for $61 \%$ of the lines and is close to 1.25 in average, which is consistent with the fact that we used $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ line intensities provided by HITRAN to determine the isotopic composition of our sample and scale the $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ absolute line intensities. The dispersion of the ratio values is not fully satisfactory, in particular for the weakest lines where it reaches a value of 2 . This results from a combined effect of the poorer experimental accuracy and a probable worsening of the quality of the intensity predictions.

## 5. Conclusion

The weak absorption spectrum of an ${ }^{18} \mathrm{O}$ enriched sample of water has been recorded by ICLAS in the region of the sec-
ond decade of vibrational states ( $11520-12820 \mathrm{~cm}^{-1}$ ). The multiplex advantage of this technique allows for a high data acquisition speed which, combined with a high sensitivity, makes it particularly well suited for the absorption spectroscopy of less abundant isotopologues.

The $\mathrm{H}_{2}{ }^{18} \mathrm{O}$ spectrum was assigned on the basis of the high accuracy variational calculations [19,20]. A set of 386 new energy levels belonging to 6 highly excited rovibrational states has been derived. The important set of new energy levels which could be retrieved will be valuable for a further refinement of the potential energy surface of this water isotopologue.

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## Appendix A. Supplementary data

Supplementary data for this article are available on ScienceDirect (www.sciencedirect.com) and as part of the Ohio State University Molecular Spectroscopy Archives (http://msa.lib.ohio-state.edu/jmsa_hp.htm).

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[^1]:    ${ }^{\text {a }}$ The vibrational term values marked by * are those calculated by Schwenke and Partridge [19] for the $0_{0,0}$ rotational level. The other values are experimental values presently determined (except for the value of the (003) state which is reproduced from Ref. [3]).

[^2]:    Note. $N$ is the number of lines used for the upper energy level determination, $\sigma$ denotes the corresponding standard deviation calculated for energies determined from more than one transition in $10^{-3} \mathrm{~cm}^{-1}$ units and $\Delta$ is the deviation of the observed levels from their calculated [19] values in $10^{-3} \mathrm{~cm}^{-1}$. Levels marked by * are in disagreement with those reported in Ref. [5].

